

## Nonparametric Counterfactual Predictions in Neoclassical Models of International Trade<sup>†</sup>

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*We develop a methodology to construct nonparametric counterfactual predictions, free of functional form restrictions on preferences and technology, in neoclassical models of international trade. First, we establish the equivalence between such models and reduced exchange models in which countries directly exchange factor services. This equivalence implies that, for an arbitrary change in trade costs, counterfactual changes in the factor content of trade, factor prices, and welfare only depend on the shape of a reduced factor demand system. Second, we provide sufficient conditions under which estimates of this system can be recovered nonparametrically. Together, these results offer a strict generalization of the parametric approach used in so-called gravity models. Finally, we use China's recent integration into the world economy to illustrate the feasibility and potential benefits of our approach. (JEL C51, D51, F11, F14, O19, P33)*

Many interesting questions in international economics are counterfactual ones. Consider China's recent export boom. In the last two decades, its share of world exports has increased from 3 percent in 1995 to 11 percent in 2011. What if it had not? What would have happened to other countries around the world?

Given the challenges inherent in isolating quasi-experimental variation in general equilibrium settings, the standard approach to answering such questions has been to proceed in three steps. First, fully specify a parametric model of preferences, technology, and trade costs around the world. Second, estimate the model's supply- and demand-side parameters. And finally, armed with this complete knowledge of

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the world economy, predict what would happen if some of the model's parameters were to change. Such computational general equilibrium (CGE) models have long been used to answer a stream of essential counterfactual questions: see, e.g., Hertel (2013) for a survey of the influential Global Trade Analysis Project (GTAP) model. Over the last ten years or so, this tradition has been enhanced by an explosion of quantitative work based on gravity models, triggered in large part by the seminal work of Eaton and Kortum (2002).

A key difference between traditional CGE models, like GTAP, and more recent CGE models, like Eaton and Kortum (2002), is parsimony. The latest version of the GTAP model described in Hertel et al. (2012) has more than 13,000 structural parameters. Counterfactual analysis in the Eaton and Kortum (2002) model can be conducted using knowledge of only one: the trade elasticity. Parsimony is valuable. But it hinges on strong functional form assumptions that may hinder the credibility of counterfactual predictions. The goal of this paper is to explore the extent to which one may maintain parsimony, but dispense with functional form assumptions. In a nutshell, can we relax Eaton and Kortum's (2002) strong functional form assumptions without circling back to GTAP's 13,000 parameters?

Our starting point is the equivalence between neoclassical economies and *reduced exchange economies* in which countries simply trade factor services. Formally, we consider a world economy comprising a representative agent in each country, constant returns to scale in production, and perfect competition in all markets. In this general environment we show that for any competitive equilibrium there is an equilibrium in a reduced exchange economy that is equivalent in terms of welfare, factor prices, and the factor content of trade and, further, that the converse is also true.

This equivalence is important for its simplifying power: a reduced exchange economy in which countries act as if they trade factor services can be characterized fully by an analysis of the *reduced factor demand system* that summarizes all agents' preferences over factor services. Thus, for a number of counterfactual questions, like the effects of uniform changes in trade costs, one does not need the complete knowledge of demand and production functions across countries and industries. For instance, one does not need to know the cross-price elasticity between French compact cars and Italian cotton shirts or between Korean flat screen TVs and Spanish heirloom tomatoes. Similarly, one does not need to know the productivity and cross-price elasticities between factors of production in each of these economic activities. All one needs to know is the implied cross-price elasticity between factor services from different countries.

This basic observation encapsulates how we propose to reduce the dimensionality of what needs to be estimated for counterfactual analysis without imposing strong functional form assumptions. Our point is not that one should focus on the reduced factor demand system because there are more goods than factors in the world, as commonly assumed in CGE models. Indeed, the previous equivalence result does not rely on this restriction. Our point is that instead of separately estimating as many demand functions as there are countries in the world and as many production functions as there are goods and countries in the world, one only needs to estimate the reduced demand for factors in each country.<sup>1</sup>

<sup>1</sup>This is not to say that assumptions about the number of factors are irrelevant for our purposes. Clearly, the fewer factors there are, the easier the estimation of the reduced factor demand system is. Note, however, that the

Our second theoretical result establishes that knowledge of this demand system as well as measures of the factor content of trade and factor payments in some initial equilibrium are sufficient to construct counterfactual predictions about the effect of changes in trade costs and factor endowments. This result provides a nonparametric generalization of the methodology popularized by Dekle, Eaton, and Kortum (2008). Their analysis focuses on a Ricardian economy in which the reduced labor demand system takes the constant elasticity of substitution (CES) form, but our result demonstrates how this functional form assumption is unnecessary.

The procedure that we propose to make counterfactual predictions relies on knowledge of the reduced factor demand system. In gravity models, such systems are implicitly assumed to be CES. Hence, a single trade elasticity can be estimated by regressing the log of bilateral flows on an exogenous shifter of the log of bilateral trade costs, like tariffs or freight costs. Our final set of theoretical results demonstrates that this approach can be pushed further than previously recognized. Namely, we provide sufficient conditions—most crucially, that the reduced factor demand system is invertible—under which, given measures of the factor content of trade and observable shifters of trade costs, reduced factor demand systems can be nonparametrically identified using the same exclusion restrictions. As with our counterfactual results, this implies that strong functional form assumptions can be dispensed with.

We conclude our paper by applying our general results to one particular counterfactual question: what would have happened to other countries if China had remained closed? In practice, data limitations are severe—Leamer’s (2010) elusive land of “Asymptopia” is far away—and estimation of a reduced factor demand system must, ultimately, proceed parametrically. So the final issue that needs to be tackled is how to parametrize and estimate a reduced factor demand system without taking a stance on particular microfoundations. We offer the following rules of thumb: (i) be as flexible as possible given data constraints; (ii) allow flexibility along the dimensions that are more likely to be relevant for the counterfactual question of interest; and (iii) use the source of variation in the data under which demand is nonparametrically identified.

Toward this goal in the present context, we introduce a strict generalization of CES, which we refer to as *mixed CES*, inspired by the work of Berry (1994) and Berry, Levinsohn, and Pakes (1995) in industrial organization.<sup>2</sup> Like in a standard gravity model, we assume the existence of a composite factor in each country so that the factor content of trade between any pair of countries is equal to their bilateral trade flow. Compared to a standard gravity model, however, our demand system features two new structural parameters that measure the extent to which exporters that are closer in terms of either market shares or some observable characteristic, which we take to be GDP per capita, tend to be closer substitutes. Under CES, when China

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same is true about the estimation of production functions in the standard approach. If one does not impose any restriction on input-output linkages across countries, a case we consider in Section IIIC, then production functions have exactly the same number of arguments as our reduced factor demand functions, that is, the total number of factors in the world.

<sup>2</sup>In their original paper on the CES function, Arrow et al. (1961, p. 230) note that one of its attractive features is that it is “the most general function which can be computed on a suitable slide rule.” Thankfully, computing power has since improved.

gains market share, Indian and French exports must be affected equally. By contrast, the mixed CES demand system allows data to speak to whether this independence of irrelevant alternatives (IIA) embodied in CES holds empirically.

Our mixed CES demand system is closely related to the nested CES demand system implied by standard multisector models in the field: see, e.g., Costinot, Donaldson, and Komunjer (2012) and Caliendo and Parro (2015). While both demand systems imply departures from IIA, the crucial distinction between our approach and existing ones is the source of variation used for estimation. We use aggregate data on factor spending shares, which are sufficient to identify the aggregate factor demand function, rather than sector-level data, which are not. Intuitively, spending shares within each sector are sufficient to identify factor demand relations at the sector level—this is what sector-level gravity equations uncover—but they cannot be used to identify factor demand relations between sectors.

Up to this point, we have emphasized the feasibility and potential benefits of our new approach to counterfactual and welfare analysis. It should be clear that our approach also has important limitations. We discuss these further below but four deserve emphasis here. First, the equivalence result on which we build heavily relies on the efficiency of perfectly competitive markets. This does not mean that our approach will necessarily fail if one were to relax the assumption of perfect competition or introduce distortions—indeed, Arkolakis, Costinot, and Rodríguez-Clare (2012) and Arkolakis et al. (2012) offer examples in this vein that cover a number of influential modeling approaches—but it is fair to say that it is much less likely to be useful in such circumstances. Second, the scope of the counterfactual exercises that we consider is limited by the restriction that the shape of the reduced demand system remains stable. Uniform changes in iceberg trade costs satisfy this condition, but many interesting shocks do not, a point we come back to in Section IIIC. Third, the restriction that the demand system is invertible implicitly excludes zeros in bilateral factor trade. So our nonparametric approach does not solve the “zeros issue” in standard gravity models.<sup>3</sup> Fourth, the estimation of a reduced factor demand system requires that the factor content of trade be measured accurately. Since the seminal work of Leontief (1953), multiple generations of trade economists have combined input-output matrices with trade data to do so, but the high level of aggregation of such matrices leaves open the possibility of mismeasurement, a point emphasized more recently by Burstein and Vogel (forthcoming).<sup>4</sup>

<sup>3</sup>This is a version of the *new goods problem* that is common in many demand settings (Bresnahan and Gordon 2008). Just as in those settings, one can typically place a lower bound on the welfare effects of a counterfactual by requiring that zeros cannot become positive. For our purposes, the more specific question is whether the challenge posed by zeros in the data is alleviated or worsened by the study of reduced factor demand relative to standard gravity approaches. The answer depends on the assumptions that one makes about the number of goods and factors. If one assumes the existence of a composite factor in each country, as we do in our empirical analysis, then focusing on factor demand reduces the prevalence of zeros relative to any analysis that would focus on trade in goods.

<sup>4</sup>In particular, national input-output matrices do not disaggregate factor payments by destination within each producing country-industry cell. The implicit assumption used to measure the factor content of trade in the empirical literature therefore is that factor intensity is constant across destinations. The previous observation notwithstanding, one should not conclude that estimating factor demand (which requires imperfect data on the factor content of trade) is necessarily more problematic than estimating goods demand and production functions (which does not require such data). Focusing on factor demand does not create new measurement issues, it merely makes existing ones more explicit. Specifically, if firms' production functions do vary by destination in practice, then assuming away such variation when estimating production functions directly would lead to the same (incorrect) counterfactual predictions as one would obtain when estimating factor demand using data on the factor content of trade that

The rest of our paper is organized as follows. Section I discusses the related literature. Section II establishes our main equivalence result. Section III uses this result to conduct counterfactual and welfare analysis. Section IV provides sufficient conditions for nonparametric identification. Section V estimates factor demand. Section VI uses these estimates to study the consequences of China's integration with the rest of the world. Section VII offers some concluding remarks.

## I. Related Literature

This paper combines old ideas from general equilibrium theory with recent methods from industrial organization and international trade to develop a new way of constructing counterfactual predictions in an open economy.

From the general equilibrium literature, we borrow the idea that, for many purposes, production economies may be reduced to exchange economies: see, e.g., Taylor (1938); Rader (1972); and Mas-Colell (1991). Early applications of this idea to international trade can be found in Meade (1952); Helpman (1976); Woodland (1980); Wilson (1980); and Neary and Schweinberger (1986). Among those, Helpman (1976); Wilson (1980); and Neary and Schweinberger (1986) are most closely related. Helpman (1976) shows how to reduce computation time necessary to solve for trade equilibria by focusing on the excess demand for factors, whereas Neary and Schweinberger (1986) introduce the concept of direct and indirect factor trade utility functions and use revealed-preference arguments to generalize the Heckscher-Ohlin Theorem. Finally, Wilson (1980) demonstrates that the analysis of the Ricardian model can be reduced to the analysis of an exchange model in which each country trades its own labor for the labor of other countries.

One can think of the starting point of our paper as a generalization of Wilson's (1980) equivalence result to any neoclassical trade model. Compared to the aforementioned papers, our main contribution is to show how the equivalence between neoclassical trade models and exchange models can be used as a tool for counterfactual and welfare analysis using commonly available data on trade flows, factor payments, and trade costs. Here, reduced exchange models are a first step toward measurement and estimation, not an analytical device for studying the theoretical properties of competitive equilibria. In this regard, our analysis bears some connection to the hedonic approach of Lancaster (1966) and Rosen (1974), with unit factor requirements and reduced factor demand playing a role similar to that of goods' characteristics and characteristics demand, respectively.<sup>5</sup>

We view our paper as a bridge between the recent gravity literature, reviewed in Costinot and Rodríguez-Clare (2014) and Head and Mayer (2014), and the older

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are constructed under the (incorrect) assumption that factor intensity is constant across destinations. Empirically, the existence of multidestination firms leads to the exact same issues as multiproduct firms: see, e.g., de Loecker et al. (2016). We discuss potential ways to make progress on these issues in Section IVA.

<sup>5</sup>Compared to standard goods' characteristics in a hedonic model, like horsepower for cars or fiber content for cereals, an attractive feature of the current setting is that there is substantial policy interest in the prices of these characteristics themselves, e.g., the wages of skilled and unskilled workers. We note, however, that unlike standard goods' characteristics in a hedonic model, factors used in the production of each good may vary in a neoclassical trade model. Even in a Ricardian model with fixed unit labor requirements, a good may be produced in a different country, and thus use a different type of labor, in response to a change in relative wages.



neoclassical trade literature, synthesized in Dixit and Norman (1980).<sup>6</sup> With the former, we share an interest in combining theory and data to shed light on counterfactual questions. With the latter, we share an interest in robust predictions, free of strong functional form assumptions. Since data are limited, there is a tension between these two goals. To make progress on the first, without giving up on the second, we therefore propose to use factor demand as a sufficient, albeit potentially high dimensional, statistic. This strategy can be thought of as a nonparametric generalization of Arkolakis, Costinot, and Rodríguez-Clare's (2012) approach to counterfactual and welfare analysis. Ultimately, there is nothing special about gravity models. They are factor demand systems, like any other neoclassical trade model. And like any demand system, factor demand systems can be estimated using data on quantities, prices, and some instrumental variables. Once this basic econometric issue is recognized, it becomes natural to turn to the recent results on the nonparametric identification of demand in differentiated markets: see, e.g., Berry, Gandhi, and Haile (2013) and Berry and Haile (2014).

Our analysis is also related to the large empirical literature on the determinants of the factor content of trade. A long and distinguished tradition—e.g., Bowen, Leamer, and Sveikauskas (1987); Trefler (1993, 1995); and Davis and Weinstein (2001)—aims to test the Heckscher-Ohlin-Vanek model by comparing the factor content of trade measured in the data to the one predicted by the model under various assumptions about technology, preferences, and trade costs (or lack thereof). Our goal is instead to estimate a factor demand system and use these estimates to conduct counterfactual and welfare analysis. In order to test or assess the fit of the Heckscher-Ohlin-Vanek model in some observed equilibrium, one does not need to know the cross-price elasticities between factors from different countries. Indeed, such tests are often conducted under the assumption that factor price equalization holds, up to some factor-augmenting productivity differences, so that factors from different countries are actually assumed to be perfect substitutes. For our purposes, knowledge of cross-price elasticities is critical.

Finally, our work provides theoretical foundations for factor-content-based analysis of the relationship between international trade and inequality in general equilibrium: see, e.g., Deardorff and Staiger (1988); Krugman (2000); and Leamer (2000). In our analysis, measures of the factor content of trade are required to estimate the reduced factor demand system as well as to generate counterfactual predictions—such as what would have happened to domestic factor prices in the absence of changes in trade costs—given knowledge of that system. Ultimately, whether large changes in the factor content of trade should tend to be associated with large changes in inequality depends on how large the own-price and cross-price elasticities between factors from different countries are. We view the estimation of these elasticities in economies with multiple factors of production as an important area for future research.<sup>7</sup>

<sup>6</sup>Further results about the theoretical properties of gravity models, including sufficient conditions for existence and uniqueness of equilibria, can be found in Allen, Arkolakis, and Takahashi (2014).

<sup>7</sup>Throughout the "trade and wages" debate in the 1990s, both labor and trade economists focused on two factors of production, skilled and unskilled labor. While one could envision finer partitions, it seems clear in this context that the number of factors is substantially lower than the number of goods, making our focus on the reduced demand for factors particularly attractive.

## II. Neoclassic Trade Models as Exchange Models

### A. Neoclassical Trade Model

Consider a world economy comprising  $i = 1, \dots, I$  countries,  $k = 1, \dots, K$  goods, and  $n = 1, \dots, N$  primary factors of production. Factor supply is inelastic:  $\mathbf{v}_i \equiv \{v_i^n\}$  denotes the vector of factor endowments in country  $i$ .

*Preferences.*—In each country  $i$ , there is a representative agent with utility

$$u_i = u_i(\mathbf{q}_i),$$

where  $\mathbf{q}_i \equiv \{q_{ji}^k\}$  is the vector of quantities consumed in country  $i$  and  $u_i$  is strictly increasing, quasiconcave, and differentiable. The previous notation allows, but does not require,  $u_i$  to depend only on  $\{\sum_j q_{ji}^k\}$ . Hence, we explicitly allow, but do not require, goods produced in different countries to be imperfect substitutes. Compared to recent quantitative work in the field, we impose no functional form assumptions on  $u$ , though the assumption of a representative agent is by no means trivial.

*Technology.*—Production is subject to constant returns to scale. Output of good  $k$  in country  $i$  that is available for consumption in country  $j$  is given by

$$q_{ij}^k = f_{ij}^k(\mathbf{I}_{ij}^k),$$

where  $\mathbf{I}_{ij}^k \equiv \{I_{ij}^{nk}\}$  is the vector of factors used to produce good  $k$  in country  $i$  for country  $j$ , and  $f_{ij}^k$  is strictly increasing, concave, differentiable, and homogeneous of degree 1.

Compared to recent quantitative work in the field, we again impose no functional form assumptions on  $f_{ij}^k$ . For instance, it is standard in the existing literature to assume that the difference between production functions across different destinations derive from iceberg trade costs that are constant across goods. This special case corresponds to the existence of Hicks-neutral productivity shifters,  $\tau_{ij}$ , such that

$$f_{ij}^k(\mathbf{I}_{ij}^k) \equiv f_i^k(\mathbf{I}_{ij}^k)/\tau_{ij}.$$

In an Arrow-Debreu sense, a good in our economy formally corresponds to a triplet  $(i, j, k)$ , whereas a factor formally corresponds to a pair  $(i, n)$ , with the usual wide interpretation. Though we impose constant returns to scale, decreasing returns in production can be accommodated in the usual way by introducing additional primary factors of production. Endogenous labor supply can be dealt with by treating leisure as another nontradable good.<sup>8</sup> Multinational production, as in Ramondo and Rodríguez-Clare (2013), can also be accommodated by expanding the set of goods and using a different index  $k$  for goods whose *technologies* originate in different

<sup>8</sup>Nontradable goods correspond to the limit case where  $f_{ij}^k$  goes to zero for all  $i \neq j$ .

countries. Finally, the assumption of no joint production can be relaxed substantially. The key requirement for our equivalence result is that there is no component of production that is joint across destination markets, as would be the case in the presence of fixed costs of production.<sup>9</sup> Besides the absence of increasing returns in each sector, the only substantial restriction imposed on technology is the absence of intermediate goods. We discuss how to incorporate such goods in Section IIIC.

*Competitive Equilibrium.*—Goods markets and factor markets are perfectly competitive. We let  $p_{ij}^k$  denote the price of good  $k$  from country  $i$  in country  $j$  and  $w_i^n$  denote the price of factor  $n$  in country  $i$ . Letting  $\mathbf{q} \equiv \{\mathbf{q}_i\}$ ,  $\mathbf{l} \equiv \{\mathbf{l}_{ij}^k\}$ ,  $\mathbf{p} \equiv \{p_{ij}^k\}$ , and  $\mathbf{w} \equiv \{w_i^n\}$ , we can then define a competitive equilibrium as follows.

DEFINITION 1: A competitive equilibrium corresponds to  $(\mathbf{q}, \mathbf{l}, \mathbf{p}, \mathbf{w})$  such that

(i) consumers maximize their utility:

$$(1) \quad \mathbf{q}_i \in \arg \max_{\tilde{\mathbf{q}}_i} u_i(\tilde{\mathbf{q}}_i),$$

$$(2) \quad \sum_{j,k} p_{ji}^k \tilde{q}_{ji}^k \leq \sum_n w_i^n \nu_i^n \quad \text{for all } i;$$

(ii) firms maximize their profits:

$$(3) \quad \mathbf{l}_{ij}^k \in \arg \max_{\tilde{\mathbf{l}}_{ij}^k} p_{ij}^k f_{ij}^k(\tilde{\mathbf{l}}_{ij}^k) - \sum_n w_i^n \tilde{l}_{ij}^{nk} \quad \text{for all } i, j, \text{ and } k;$$

(iii) good markets clear:

$$(4) \quad q_{ij}^k = f_{ij}^k(\mathbf{l}_{ij}^k) \quad \text{for all } i, j, \text{ and } k;$$

(iv) factor markets clear:

$$(5) \quad \sum_{j,k} l_{ij}^{nk} = \nu_i^n \quad \text{for all } i \text{ and } n.$$

### B. Reduced Exchange Model

An old idea in general equilibrium theory is that it is often simpler to analyze the competitive equilibrium of a neoclassical model with production by studying instead a fictitious endowment economy in which consumers directly exchange factor services: see, e.g., Taylor (1938); Rader (1972); and Mas-Colell (1991). Although this idea is often associated in the trade literature with the Heckscher-Ohlin model, it applies equally well to the Ricardian model of trade: see, e.g., Wilson (1980). We now offer a formal proof of the equivalence between a general neoclassical trade

<sup>9</sup>This implies that our theoretical framework can accommodate economies in which there are multiple regions within a country and firms in each region jointly produce goods and amenities.



model and an exchange economy, in terms of the factor content of trade, factor prices, and welfare. This equivalence result will be the backbone of our approach to counterfactual and welfare analysis in Section III.

Starting from the neoclassical trade model of Section IIA, we can define the reduced utility function over primary factors of production in country  $i$  as

$$(6) \quad U_i(\mathbf{L}_i) \equiv \max_{\tilde{\mathbf{q}}_i, \tilde{\mathbf{l}}_i} u_i(\tilde{\mathbf{q}}_i),$$

$$(7) \quad \tilde{q}_{ji}^k \leq f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) \quad \text{for all } j \text{ and } k,$$

$$(8) \quad \sum_k \tilde{l}_{ji}^{nk} \leq L_{ji}^n \quad \text{for all } j \text{ and } n,$$

where  $\mathbf{L}_i \equiv \{L_{ji}^n\}$  denotes the vector of total factor demands from country  $i$ . It describes the maximum utility that a consumer in country  $i$  would be able to achieve if she were endowed with  $\mathbf{L}_i$  and had access to the technologies of all firms around the world.<sup>10</sup> One can check that  $U_i(\cdot)$  is strictly increasing and quasiconcave, though not necessarily strictly quasiconcave, even if  $u_i(\cdot)$  is.<sup>11</sup> In particular,  $U_i(\cdot)$  is likely to be linear whenever production functions are identical around the world. While this situation is obviously knife-edge, this is the special case on which the Heckscher-Ohlin model of trade focuses. We therefore explicitly allow for such situations below.

Letting  $\mathbf{L} \equiv \{\mathbf{L}_i\}$ , we can define a competitive equilibrium of the reduced exchange model or, in short, a reduced equilibrium.

DEFINITION 2: A reduced equilibrium corresponds to  $(\mathbf{L}, \mathbf{w})$  such that

(i) consumers maximize their reduced utility:

$$(9) \quad \mathbf{L}_i \in \arg \max_{\tilde{\mathbf{L}}_i} U_i(\tilde{\mathbf{L}}_i),$$

$$\sum_{j,n} w_j^n \tilde{L}_{ji}^n \leq \sum_n w_i^n v_i^n \quad \text{for all } i;$$

<sup>10</sup>The definition above is closely related to, but distinct from, the notion of the *direct factor trade utility function* introduced in Neary and Schweinberger (1986). The distinction comes from the fact that Neary and Schweinberger's (1986) factor trade utility function measures the maximum utility attainable if all consumption must be produced using the techniques of the home country. In our definition, each country is assumed to have access to the techniques in all other countries, inclusive of trade costs. This distinction is important. As we will show in a moment, the factor content of trade derived from solving (6) coincides with the factor content of trade in the competitive equilibrium. This would no longer be true if one were to maximize Neary and Schweinberger's (1986) factor trade utility function.

<sup>11</sup>The fact  $U_i$  is strictly increasing in  $\mathbf{L}_i$  is trivial. To see that  $U_i$  is quasiconcave, take two vectors of factor demand,  $\mathbf{L}_i$  and  $\tilde{\mathbf{L}}_i$ , and  $\alpha \in [0, 1]$ . Let  $(\mathbf{q}, \mathbf{l})$  and  $(\tilde{\mathbf{q}}, \tilde{\mathbf{l}})$  be the solution of (6) associated with  $\mathbf{L}_i$  and  $\tilde{\mathbf{L}}_i$ , respectively. Now consider  $(\bar{\mathbf{q}}, \bar{\mathbf{l}}) \equiv \alpha(\mathbf{q}, \mathbf{l}) + (1 - \alpha)(\tilde{\mathbf{q}}, \tilde{\mathbf{l}})$ . By construction,  $\bar{\mathbf{l}}$  trivially satisfies (8). Since  $f_{ji}^k$  is concave, we also have  $\bar{q}_{ji}^k \leq \alpha f_{ji}^k(\mathbf{l}_{ji}^k) + (1 - \alpha)f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) \leq f_{ji}^k(\bar{\mathbf{l}}_{ji}^k)$  for all  $j$  and  $k$ . This implies  $U_i(\alpha \mathbf{L}_i + (1 - \alpha)\tilde{\mathbf{L}}_i) \geq u_i(\bar{\mathbf{q}}) \geq \min\{u_i(\mathbf{q}), u_i(\tilde{\mathbf{q}})\} = \min\{U_i(\mathbf{L}_i), U_i(\tilde{\mathbf{L}}_i)\}$  where the second inequality follows from the quasiconcavity of  $u_i$ .

(ii) factor markets clear:

$$(10) \quad \sum_j L_{ij}^n = \nu_i^n \quad \text{for all } i \text{ and } n.$$

Our main equivalence result can be stated as follows.

**PROPOSITION 1:** *For any competitive equilibrium  $(\mathbf{q}, \mathbf{l}, \mathbf{p}, \mathbf{w})$ , there exists a reduced equilibrium  $(\mathbf{L}, \mathbf{w})$  with: (i) the same factor prices,  $\mathbf{w}$ ; (ii) the same factor content of trade,  $L_{ij}^n = \sum_k l_{ij}^{nk}$  for all  $i, j$ , and  $n$ ; and (iii) the same welfare levels,  $U_i(\mathbf{L}_i) = u_i(\mathbf{q}_i)$  for all  $i$ . Conversely, for any reduced equilibrium,  $(\mathbf{L}, \mathbf{w})$ , there exists a competitive equilibrium,  $(\mathbf{q}, \mathbf{l}, \mathbf{p}, \mathbf{w})$ , such that conditions (i)–(iii) hold.*

The formal proof of Proposition 1 can be found in Appendix A. The basic arguments are similar to those used in proofs of the First and Second Welfare Theorems. This should be intuitive. In the reduced equilibrium, each representative agent solves a country-specific planning problem, as described in (6). Thus, showing that any competitive equilibrium is associated with an equivalent reduced equilibrium implicitly relies on the efficiency of the original competitive equilibrium, which the First Welfare Theorem establishes. Similarly, showing that any reduced equilibrium is associated with an equivalent competitive equilibrium implicitly relies on the ability to decentralize efficient allocations, which the Second Welfare Theorem establishes. The key distinction between Proposition 1 and standard Welfare Theorems is that the reduced equilibrium is not a global planner's problem; it remains a decentralized equilibrium in which countries fictitiously trade factor services and budgets are balanced country by country. Broadly speaking, we do not go all the way from the decentralized equilibrium to the global planner's problem, but instead stop at a hybrid reduced equilibrium, which combines country-specific planner's problems with perfect competition in factor markets.<sup>12</sup>

According to Proposition 1, if one is interested in the factor content of trade, factor prices, or welfare, then one can always study a reduced equilibrium—whose primitives are the reduced utility functions,  $\{U_i\}$ , and the endowments,  $\{\nu_i\}$ —rather than a competitive equilibrium—whose primitives are the utility functions,  $\{u_i\}$ , the endowments,  $\{\nu_i\}$ , and the production functions,  $\{f_{ij}^k\}$ . In order to do counterfactual and welfare analysis, one does not need to have *direct* knowledge of both the utility functions,  $\{u_i\}$ , and the production functions,  $\{f_{ij}^k\}$ . Instead, one merely needs to

<sup>12</sup>This implies, in particular, that the convexity of preferences and technology, which is central in the proof of the Second Welfare Theorem, plays no role in the proof of Proposition 1. In the Second Welfare Theorem, convexity is invoked for Lagrange multipliers, and in turn, competitive prices, to exist. Here, competitive prices for goods can be directly constructed from factor prices in the reduced equilibrium using zero-profit conditions. Note also that since Proposition 1 relies on the efficiency of the competitive equilibrium, we expect a version of the previous result to hold under alternative market structures provided that the decentralized equilibria are Pareto efficient, like under monopolistic competition with CES utility; see Dhingra and Morrow (2016). The only additional issue that needs to be dealt with in imperfectly competitive environments is the presence of fixed costs of entry that are a source of joint production across destinations, as mentioned in Section IIA. One way to sidestep this issue is to focus on a reduced utility function over primary factors of production, and hence factor demand, that is conditional on the measure of entrants in all countries. This is the approach used implicitly by Arkolakis, Costinot, and Rodríguez-Clare (2012) when defining CES import demand systems in the context of gravity models.

know how they *indirectly* shape,  $\{U_i\}$ , and in turn global factor demand; that is, the solution of the reduced utility maximization problem (9).<sup>13</sup>

### III. Counterfactual and Welfare Analysis

We start by considering counterfactual shocks to preferences and factor endowments in a reduced exchange model. In this context, we show how to extend the exact hat algebra popularized by Dekle, Eaton, and Kortum (2008) in the context of a CES demand system to general, non-CES environments. Perhaps surprisingly, the critical assumption required for the previous approach to succeed is the knowledge of the factor demand system, not strong functional form assumptions on its shape. Using the equivalence result from Section II, we then show how the previous counterfactual predictions can be used to study the effect of changes in endowments and technology in a general neoclassical model of trade.

#### A. Reduced Counterfactuals

Consider a reduced exchange model in which the reduced utility function over primary factors is parametrized such that

$$(11) \quad U_i(\mathbf{L}_i) = \bar{U}_i(\{L_{ji}^n/\tau_{ji}^n\}),$$

where  $\bar{U}_i$  is a strictly increasing and quasiconcave utility function and  $\tau_{ji}^n > 0$  are exogenous preference shocks. The counterfactual question that we are interested in here is: what are the effects of a change from  $(\tau, \nu) \equiv \{\tau_{ji}^n, \nu_i^n\}$  to  $(\tau', \nu') \equiv \{(\tau'_{ji})', (\nu_i')'\}$  on trade flows, factor prices, and welfare?<sup>14</sup>

*Trade Flows and Factor Prices.*—For each country  $i$ , let  $\mathbf{L}_i(\mathbf{w}, y_i | \tau)$  denote the set of solutions to the utility maximization problem (9) as a function of factor prices,  $\mathbf{w}$ , income,  $y_i \equiv \sum_n w_i^n \nu_i^n$ , and preference parameters,  $\tau$ . This corresponds to the Marshallian demand for factor services in the reduced equilibrium. The associated vectors of factor expenditure shares are then given by

$$\chi_i(\mathbf{w}, y_i | \tau) \equiv \{ \{x_{ji}^n\} | x_{ji}^n = w_j^n L_{ji}^n / y_i \text{ for some } \mathbf{L}_i \in \mathbf{L}_i(\mathbf{w}, y_i | \tau) \}.$$

Since preference shocks are multiplicative, expenditure shares must depend only on the *effective* factor prices,  $\omega_i \equiv \{w_j^n \tau_{ji}^n\}$ . We can therefore write, with a slight abuse of notation and without risk of confusion,  $\chi_i(\mathbf{w}, y_i | \tau) \equiv \chi_i(\omega_i, y_i)$ . In what follows

<sup>13</sup>This is true regardless of whether the competitive and reduced equilibria are unique. Formally, Proposition 1 establishes that the set of factor prices, factor content of trade, and welfare levels that can be observed in a competitive equilibrium is the same as the set of factor prices, factor content of trade, and welfare levels that can be observed in a reduced equilibrium. Whether the previous sets are singletons is irrelevant for our equivalence result.

<sup>14</sup>One can always trivially write the function  $U_i(\mathbf{L}_i)$  as it appears in equation (11). Hence, there is no restriction on the set of preferences that we consider here nor on the set of neoclassical models that we will consider in Section IIIB. The only restriction that we impose is on the preference shocks that all enter equation (11) multiplicatively. We will impose the same restriction on trade cost shocks in equation (20).

we refer to  $\chi_i$  as the factor demand system in country  $i$ . Using the previous notation, the equilibrium conditions (9) and (10) can then be expressed compactly as

$$\mathbf{x}_i \in \chi_i(\omega_i, y_i) \quad \text{for all } i,$$

$$\sum_j x_{ij}^n y_j = y_i^n, \quad \text{for all } i \text{ and } n,$$

where  $\mathbf{x}_i \equiv \{x_{ji}^n\}$  denotes the vector of factor expenditure shares in country  $i$  and  $y_i^n \equiv w_i^n \nu_i^n$  denotes payments to factor  $n$ . Note also that we can always, and without loss of generality, choose the location of preference shocks in equation (11) so that effective factor prices in the initial equilibrium are equal to 1 in all countries,

$$(12) \quad \omega_{ji}^n = 1, \quad \text{for all } i, j, \text{ and } n.$$

We maintain this normalization throughout our analysis.<sup>15</sup>

A standard gravity model, such as the one developed by Anderson and van Wincoop (2003) and Eaton and Kortum (2002), corresponds to the special case in which there is only one factor of production in each country and factor demand is CES. Omitting the index for factors,  $n$ , such models require

$$(13) \quad \chi_{ji}(\omega_i, y_i) = \frac{\mu_{ji}(\omega_{ji})^\epsilon}{\sum_l \mu_{li}(\omega_{li})^\epsilon}, \quad \text{for all } j \text{ and } i,$$

for some trade elasticity  $\epsilon$ , and exogenous shifters  $\{\mu_{ji}\}$ ; see Arkolakis, Costinot, and Rodríguez-Clare (2012) and Costinot and Rodríguez-Clare (2014) for further discussion.<sup>16</sup> We now proceed under the assumption that the factor demand system  $\chi_i$  is known, but dispense with any functional form restriction.

Let  $\mathbf{x}'_i \equiv \{(x'_{ji})^n\}$  and  $\mathbf{w}'$  denote the counterfactual expenditure shares and factor prices in the counterfactual equilibrium with preference parameters and endowments given by  $(\tau', \nu')$ . The basic idea behind the exact hat algebra of Dekle, Eaton, and Kortum (2008) is to focus on the proportional changes in expenditure shares and factor prices,  $\hat{\mathbf{x}}_i \equiv \{(x'_{ji})^n/x_{ji}^n\}$  and  $\hat{\mathbf{w}} \equiv \{(w'_j)^n/w_j^n\}$ , caused by proportional changes in preferences and endowments,  $\hat{\tau} \equiv \{(\tau'_{ji})^n/\tau_{ji}^n\}$  and  $\hat{\nu} \equiv \{(\nu'_i)^n/\nu_i^n\}$ .<sup>17</sup> There is nothing in this general strategy that hinges on the demand system being CES.

<sup>15</sup>Formally, suppose that given an arbitrary decomposition of the utility function,  $U_i$ , into a reference utility function,  $\bar{U}_i$ , and preference shocks,  $\{\tau'_{ji}\}$ , the effective factor prices in the initial equilibrium,  $\{\omega_{ji}^n\}$ , are not equal to 1. Then starting from the previous prices, we can always consider an alternative decomposition  $\bar{U}_i(\{L'_{ji}\}) \equiv \bar{U}_i(\{L_{ji}^n/\omega_{ji}^n\})$  and  $\{\bar{\tau}'_{ji}\} \equiv \{\tau'_{ji}/\omega_{ji}^n\}$  so that  $U_i(L_i) = \bar{U}_i(\{L'_{ji}\}/\bar{\tau}'_{ji})$ . By construction, the effective factor prices associated with this new decomposition,  $\{\bar{\omega}_{ji}^n\}$ , must satisfy  $\bar{\omega}_{ji}^n = w_j^n \bar{\tau}'_{ji} = w_j^n \tau'_{ji}/\omega_{ji}^n = 1$  for all  $i, j$ , and  $n$ .

<sup>16</sup>In this case, total income,  $y_i$ , has no effect on factor expenditure shares because of homotheticity.

<sup>17</sup>In the rest of this paper, we restrict ourselves to equilibria such that  $x'_{ji} > 0$  for all  $i, j$ , and  $n$ . This guarantees that proportional changes between the initial and counterfactual equilibrium are well defined. Empirically, zeros are irrelevant for the sample of countries and the level of aggregation at which we will conduct our estimation and counterfactual simulation below.

Let us start by rewriting the equilibrium conditions at the counterfactual values of the preference and endowment parameters,  $(\tau', \nu')$ :

$$\mathbf{x}'_i \in \chi_i(\omega'_i, y'_i) \quad \text{for all } i,$$

$$\sum_j (x'_{ij})' y'_j = (y'_i)', \quad \text{for all } i \text{ and } n.$$

These two conditions, in turn, can be expressed in terms of proportional changes:

$$\{\hat{x}'_{ij} x'_{ij}\} \in \chi_i\left(\{\hat{w}'_j \hat{\tau}'_{ji} \omega'_{ji}\}, \sum_n \hat{w}'_i \hat{\nu}'_i y'_i\right) \quad \text{for all } i,$$

$$\sum_j \hat{x}'_{ij} x'_{ij} \left(\sum_n \hat{w}'_j \hat{\nu}'_j y'_j\right) = \hat{w}'_i \hat{\nu}'_i y'_i, \quad \text{for all } i \text{ and } n,$$

where we have used the fact that total income in the counterfactual equilibrium is equal to the sum of total factor income,  $y'_i = \sum_n (y'_i)'$ . This leads to the following proposition.

**PROPOSITION 2:** *Proportional changes in expenditure shares and factor prices,  $\hat{\mathbf{x}}_i \equiv \{(x'_{ij})'/x'_{ij}\}$  and  $\hat{\mathbf{w}} \equiv \{(w'_j)'/w'_j\}$ , caused by the proportional changes in preferences and endowments,  $\hat{\tau} \equiv \{(\tau'_{ji})'/\tau'_{ji}\}$  and  $\hat{\nu} \equiv \{(\nu'_i)'/\nu'_i\}$ , solve*

$$(14) \quad \{\hat{x}'_{ij} x'_{ij}\} \in \chi_i\left(\{\hat{w}'_j \hat{\tau}'_{ji} \omega'_{ji}\}, \sum_n \hat{w}'_i \hat{\nu}'_i y'_i\right) \quad \text{for all } i,$$

$$(15) \quad \sum_j \hat{x}'_{ij} x'_{ij} \left(\sum_n \hat{w}'_j \hat{\nu}'_j y'_j\right) = \hat{w}'_i \hat{\nu}'_i y'_i, \quad \text{for all } i \text{ and } n,$$

where the effective factor prices in the initial equilibrium,  $\omega_i \equiv \{w'_j \tau'_{ji}\}$ , are given by (12).

Once proportional changes in expenditure shares and factor prices have been solved for, the value of imports of factor  $n$  from country  $i$  in country  $j$  in the counterfactual equilibrium,  $(X'_{ij})'$ , can be simply computed as

$$(X'_{ij})' = \hat{x}'_{ij} x'_{ij} \left(\sum_n \hat{w}'_j \hat{\nu}'_j y'_j\right) \quad \text{for all } i, j, \text{ and } n.$$

To sum up, if we know the factor demand system in all countries,  $\{\chi_i\}$ , and have access to data on expenditure shares and factor payments,  $\{x'_{ij}\}$  and  $\{y'_j\}$ , then we can compute counterfactual changes in factor trade and factor prices. Using standard arguments from consumer theory, we establish next that the knowledge of  $\chi_i$  is also sufficient for computing welfare changes in country  $i$ .

*Welfare.*—Consider an arbitrary country  $i$ . We are interested in computing the equivalent variation,  $\Delta W_i$ , associated with a shock from  $(\tau, \nu)$  to  $(\tau', \nu')$ . When expressed as a fraction of country  $i$ 's initial income, this is given by

$$(16) \quad \Delta W_i = (e_i(\omega_i, U_i') - y_i)/y_i,$$

where  $U_i'$  denotes the utility level of country  $i$  in the counterfactual equilibrium and  $e_i(\cdot, U_i')$  denotes the expenditure function,

$$e_i(\omega_i, U_i') \equiv \min_{\tilde{\mathbf{L}}_i} \left\{ \sum_{n,j} \omega_{ji}^n \tilde{L}_{ji}^n \mid \bar{U}_i(\tilde{\mathbf{L}}_i) \geq U_i' \right\}.$$

By construction,  $\Delta W_i$  measures the percentage change in income that the representative agent in country  $i$  would be indifferent about accepting in lieu of the counterfactual change from  $(\tau, \nu)$  to  $(\tau', \nu')$ . Note that when preference shocks occur in country  $i$ —i.e., when there is a change from  $\tau_{ji}^n$  for some  $j$  and  $n$ —the expenditure function implicitly measures the amount of income necessary to reach  $U_i'$  given the original preferences—i.e., given utility  $\bar{U}_i(\{L_{ji}^n/\tau_{ji}^n\})$ —taking into account that after the shock the consumer maximizes  $\bar{U}_i(\{L_{ji}^n/(\tau_{ji}^n)'\})$ . Since preference shocks are multiplicative, this is equivalent to a change in effective factor prices from  $\omega_i \equiv \{w_j^n \tau_{ji}^n\}$  to  $\omega_i' \equiv \{(w_j^n)'(\tau_{ji}^n)'\}$ .

To compute  $\Delta W_i$ , we can solve a system of ordinary differential equations (ODE), as in Hausman (1981) and Hausman and Newey (1995). Since the expenditure function  $e_i(\cdot, U_i')$  is concave in the effective factor prices, it must be differentiable almost everywhere. The Envelope Theorem (e.g., Milgrom and Segal 2002, Theorem 1) therefore implies

$$de_i(\omega, U_i')/d\omega_j^n = L_{ji}^n(\omega, e_i(\omega, U_i')) \quad \text{for all } j \text{ and } n \text{ and almost all } \omega,$$

with  $\{L_{ji}^n(\omega, e_i(\omega, U_i'))\}$  that solves (9) at the effective factor prices,  $\omega$ . Given our focus on expenditure shares, it is convenient to rearrange the previous expression in logs. For any selection  $\{x_{ji}^n(\omega, y)\} \in \chi_i(\omega, y)$ , we must have

$$(17) \quad d \ln e_i(\omega, U_i')/d \ln \omega_j^n = x_{ji}^n(\omega, e_i(\omega, U_i')) \quad \text{for all } j \text{ and } n \text{ and almost all } \omega.$$

By budget balance in the counterfactual equilibrium, we also know that

$$(18) \quad e_i(\omega_i', U_i') = y_i',$$

where  $\omega_i'$  is the vector of effective factor prices in the counterfactual equilibrium.

The expenditure function  $e_i(\cdot, U_i')$  must be equal to the unique solution of (17) satisfying (18). This solution can be computed given knowledge of any selection  $\{x_{ji}^n(\cdot, \cdot)\} \in \chi_i(\cdot, \cdot)$ , country  $i$ 's income level in the counterfactual equilibrium,  $y_i' = \sum_n \hat{w}_i^n \hat{\nu}_i^n y_i^n$ , and the effective factor prices in the counterfactual equilibrium,  $\omega_i' = \{\hat{w}_j^n \hat{\tau}_{ji}^n\}$ , with  $\hat{\mathbf{w}}$  given by (14) and (15). This leads to our next proposition.



**PROPOSITION 3:** *The equivalent variation associated with a change from  $(\boldsymbol{\tau}, \boldsymbol{\nu})$  to  $(\boldsymbol{\tau}', \boldsymbol{\nu}')$ , expressed as a fraction of country  $i$ 's initial income, is*

$$(19) \quad \Delta W_i = (e(\boldsymbol{\omega}_i, U_i') - y_i)/y_i,$$

where  $\boldsymbol{\omega}_i$  is given by (12) and  $e(\cdot, U_i')$  is the unique solution of (17) and (18).

### B. Application to Neoclassical Trade Models

Our goal now is to find structural shocks in a neoclassical trade model that are isomorphic to preference and endowment shocks in a reduced exchange model. By Propositions 1–3, counterfactual predictions about factor content of trade, factor prices, and welfare in neoclassical model can then be computed using equations (12), (14), (15), and (17)–(19).

Consider a neoclassical trade model in which technology is parametrized such that

$$(20) \quad f_{ij}^k(\mathbf{1}_{ij}^k) \equiv \bar{f}_{ij}^k(\{l_{ij}^{nk}/\tau_{ij}^n\}), \quad \text{for all } i, j, \text{ and } k,$$

where  $\tau_{ij}^n$  denotes factor-augmenting productivity shocks, that are common to all goods for a given exporter-importer pair. Since these productivity shocks are bilateral in nature, we simply refer to them as trade cost shocks from now on.<sup>18</sup>

Given equation (20), the reduced utility function over primary factors of production associated with the present neoclassical trade model can be written as

$$U_i(\mathbf{L}_i) \equiv \max_{\tilde{\mathbf{q}}_i, \tilde{\mathbf{l}}_i} u_i(\tilde{\mathbf{q}}_i),$$

$$\tilde{q}_{ji}^k \leq \bar{f}_{ji}^k(\{\tilde{l}_{ji}^{nk}/\tau_{ji}^n\}) \quad \text{for all } j \text{ and } k,$$

$$\sum_k \tilde{l}_{ji}^{nk} \leq L_{ji}^n \quad \text{for all } j \text{ and } n.$$

A simple change of variable then implies

$$U_i(\mathbf{L}_i) \equiv \bar{U}_i(\{L_{ji}^n/\tau_{ji}^n\}),$$

<sup>18</sup>Formally, a change in iceberg trade costs between countries  $i$  and  $j$  corresponds to the special case in which productivity shocks are Hicks-neutral for a given exporter-importer pair, i.e.,  $\tau_{ij}^n = \tau_{ij}$ . Note that while the productivity shocks considered in equation (20) may not vary across goods, equation (20) does allow for a very rich set of heterogeneous trading frictions in the initial equilibrium:  $\bar{f}_{ij}^k$  may vary with both  $i$  and  $j$  for all  $k$ . Thus, some goods may be more costly to trade than others. Similarly, goods that are exported may have different factor intensity than goods that are sold domestically, as in Matsuyama (2007). Note also that the productivity shocks considered in equation (20) may vary across factors  $n$ . Hence, our model can accommodate economies in which only a subset of individuals get access to foreign markets.

with

$$\bar{U}_i(\mathbf{L}_i) \equiv \max_{\tilde{\mathbf{q}}_i, \tilde{\mathbf{l}}_i} u_i(\tilde{\mathbf{q}}_i),$$

$$\tilde{q}_{ji}^k \leq \bar{f}_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) \quad \text{for all } j \text{ and } k,$$

$$\sum_k \tilde{l}_{ji}^{nk} \leq L_{ji}^n \quad \text{for all } j \text{ and } n.$$

Thus, if technology satisfies (20),  $U_i(\cdot)$  satisfies (11). Not surprisingly, trade cost shocks in a neoclassical trade model are equivalent to preference shocks in the associated reduced exchange model. Since endowment shocks are identical in neoclassical trade models and reduced exchange models, we arrive at the following corollary of Propositions 1–3.

**COROLLARY 1:** *Proportional changes in the factor content of trade, factor prices, and welfare caused by trade cost shocks and endowment shocks in a neoclassical trade model,  $\hat{\tau} \equiv \{(\tau_{ji}^n)'/\tau_{ji}^n\}$  and  $\hat{\nu} \equiv \{(\nu_i^n)'/\nu_i^n\}$ , are given by (12), (14), (15), and (17)–(19).*

To sum up, equations (12), (14), (15), and (17)–(19) provide a system of equations that can be used for counterfactual and welfare analysis. It generalizes the exact hat algebra of Dekle, Eaton, and Kortum (2008) developed in the case of constant elasticity of substitution (CES) factor demands to any factor demand system. Namely, given data on expenditure shares and factor payments,  $\{x_{ji}^n\}$  and  $\{y_i^n\}$ , if one knows the factor demand system,  $\chi_i$ , then one can compute counterfactual changes in factor prices, aggregate trade flows, and welfare.<sup>19</sup> Sections IV and V discuss identification and estimation, respectively, of the factor demand system,  $\chi_i$ . Before doing so, we briefly discuss some extensions of the previous results.

### C. Extensions

*Sector-Specific Trade Cost Shocks.*—Our approach emphasizes that in any neoclassical trade model, it is as if countries were directly trading factor services. As we have shown in the previous subsection, this approach is well suited to study factor-augmenting productivity shocks, in general, and uniform changes in iceberg trade costs, in particular. While such shocks are of independent interest, they are restrictive. For instance, one may want to study trade cost shocks that only affect a subset of sectors in the economy. Here, we demonstrate how our analysis can be extended to cover such cases.

Consider the same neoclassical economy as in Section IIIB with technology satisfying (20). For expositional purposes, consider a counterfactual shock that

<sup>19</sup>Like Proposition 1, the corollary above holds whether or not a competitive equilibrium is unique. If there are multiple equilibria, then there is a set of proportional changes in the factor content of trade, factor prices, and welfare caused by  $\hat{\tau}$  and  $\hat{\nu}$ , but this set remains characterized by (12), (14), (15), and (17)–(19).

only affects productivity,  $\tau_{ij}^{nk}$ , of one factor,  $n$ , for one country pair,  $i$  and  $j$ , in a single sector,  $k$ . To study such a counterfactual scenario, we only need to add one factor and one nonarbitrage condition to our previous analysis. Namely, instead of only having “factor  $n$  in country  $i$ ,” we can define “factor  $n$  from country  $i$  that is used to produce good  $k$ ” and “factor  $n$  from country  $i$  that is not.” The price of both factors in a competitive equilibrium, of course, should be the same. Given this new set of factors, all shocks remain uniform across goods. Thus, the results of Section IIIB still apply.<sup>20</sup>

Of course, as trade cost shocks become more and more heterogeneous across sectors, our emphasis on the factor content of trade becomes less and less useful. In the extreme case where all goods are subject to a different shock, it is no simpler to study a reduced exchange model with  $K \times N$  factors in each country than the complete neoclassical trade model with  $K$  goods and  $N$  factors. The flip-side of this observation is that, away from this extreme case, our approach is always useful in the sense that it reduces the dimensionality of what needs to be estimated, i.e., the factor demand system.

*Tariffs.*—Historically, an important application of CGE models has been the analysis of regional trade agreements, such as NAFTA and the European Union, in which the counterfactual shocks of interest were not productivity shocks but rather changes in trade policy: see, e.g., Baldwin and Venables (1995) for a survey. We now discuss how our analysis can be extended to analyze the effects of changes in ad valorem trade taxes. For pedagogical purposes, it is useful to start from a reduced exchange model, as in Section IIIA, but one in which a factor  $n$  being traded between country  $i$  and country  $j$  is subject to an ad valorem import tax or subsidy,  $t_{ij}^n$ . Once this case has been dealt with, the empirically relevant case in which tariffs vary across sectors, not factors, can be dealt with by redefining factors appropriately, as we did in the case of sector-specific trade cost shocks.<sup>21</sup>

The key difference between the reduced equilibrium with and without trade taxes is that taxes raise revenue. This needs to be added to factor income in equations (14) and (15) when computing changes in factor prices and the factor content of trade. Formally, consider a change in trade taxes from  $\mathbf{t} \equiv \{t_{ij}^n\}$  to  $\mathbf{t}' \equiv \{(t_{ij}^n)'\}$ . The counterparts of equations (14) and (15) in this situation become

$$\{\hat{x}_{ji}^n x_{ji}^n\} \in \chi_i \left( \left\{ \hat{w}_j^n \left( \widehat{1 + t_{ij}^n} \right) \right\}, \hat{y}_j y_j \right) \quad \text{for all } i,$$

$$\sum_j \hat{x}_{ij}^n x_{ij}^n \hat{y}_j y_j = \hat{w}_i^n \hat{v}_i^n y_i^n, \quad \text{for all } i \text{ and } n,$$

<sup>20</sup>In the special case of economies with tradable and nontradable sectors, it should be clear that one does not need to create a new factor in order to study uniform changes in trade costs in the tradable sectors. Such shocks are equivalent to factor-augmenting productivity shocks that are uniform across both tradable and nontradable and leave all nontradable goods non-traded.”

<sup>21</sup>Wilson (1980) discusses this issue in the context of the Ricardian model.

with total income, inclusive of tax revenues, such that

$$y_i = \sum_n \frac{y_i^n}{1 - \sum_j \sum_n t_{ji}^n x_{ji}^n / (1 + t_{ji}^n)} \quad \text{for all } i,$$

$$\hat{y}_i y_i = \sum_n \frac{\hat{w}_i^n \hat{v}_i^n y_i^n}{1 - \sum_j \sum_m (t_{ji}^m)' \hat{x}_{ji}^m x_{ji}^m / (1 + t_{ji}^m)'} \quad \text{for all } i.$$

Equations (17)–(19) are unchanged. So, given information on tariffs,  $\mathbf{t}$  and  $\mathbf{t}'$ , changes in the factor content of trade, factor prices, and welfare can still be computed using only: (i) data on initial expenditure shares and factor payments,  $\{x_{ij}^n\}$  and  $\{y_j^n\}$ , and (ii) an estimate of the factor demand system,  $\chi_i$ , in each country.

*Intermediate Goods.*—The neoclassical trade model of Section II rules out intermediate goods. We conclude by discussing how our theoretical analysis can be extended to environments with input-output linkages. Consider an economy in which gross output of good  $k$  produced in country  $i$  that is available in country  $j$ —either as a final good for consumers or an intermediate good for firms—is given by

$$q_{ij}^k = f_{ij}^k(\mathbf{l}_{ij}^k, \mathbf{m}_{ij}^k),$$

where  $\mathbf{l}_{ij}^k \equiv \{l_{ij}^{nk}\}$  still denotes the vector of factor demands and  $\mathbf{m}_{ij}^k \equiv \{m_{oij}^{gk}\}$  is the vector of input demands, with  $m_{oij}^{gk}$  being the amount of good  $g$  from the origin country  $o$  that is used as an intermediate good in country  $i$  to produce good  $k$  and deliver it to country  $j$ . In a competitive equilibrium, gross output must then be equal to the total demand by consumers and firms,

$$c_{ij}^k + \sum_{l,d} m_{ijd}^{kl} = q_{ij}^k \quad \text{for all } i, j, \text{ and } k,$$

where  $\mathbf{c}_i \equiv \{c_{ji}^k\}$  denotes the vector of final demand in country  $i$ . All other assumptions are the same as in Section IIA.

In this more general environment, we can still define a reduced utility function over primary factors of production:

$$U_i(\mathbf{L}_i) \equiv \max_{\tilde{\mathbf{q}}, \tilde{\mathbf{m}}, \tilde{\mathbf{c}}, \tilde{\mathbf{l}}} u_i(\tilde{\mathbf{c}}_i),$$

$$\tilde{q}_{jd}^k \leq f_{jd}^k(\tilde{\mathbf{l}}_{jd}^k, \tilde{\mathbf{m}}_{jd}^k) \quad \text{for all } d, j, \text{ and } k,$$

$$\sum_{d,k} \tilde{l}_{jd}^{nk} \leq L_{ji}^n \quad \text{for all } j \text{ and } n,$$

$$\tilde{c}_{jd}^k + \sum_{g,r} \tilde{m}_{jdr}^{kg} \leq \tilde{q}_{jd}^k \quad \text{for all } d, j, \text{ and } k,$$

with  $\tilde{\mathbf{q}} \equiv \{\tilde{q}_{jd}^k\}$ ,  $\tilde{\mathbf{m}} \equiv \{\tilde{m}_{jdr}^{kg}\}$ ,  $\tilde{\mathbf{c}} \equiv \{\tilde{c}_{jd}^k\}$ , and  $\tilde{\mathbf{l}} \equiv \{\tilde{l}_{jd}^{nk}\}$ . Compared to the definition of Section IIB, the control variables now include gross output, intermediate goods,

final demands, and primary factors for all destination countries,  $d$ , not just country  $i$ . This reflects the potential existence of global supply chains in which factors from country  $j$  may be used to produce intermediate goods for country  $d$ , which are then used to produce final goods for country  $i$ .<sup>22</sup>

One can show that Proposition 1 still holds in this economy, with the factor content of trade being computed as in Johnson and Noguera (2012). The only technicality is that the proof now requires the Nonsubstitution Theorem to construct good prices in a competitive equilibrium from factor prices in a reduced equilibrium. Conditional on the new definition of the reduced utility function, Propositions 2 and 3 are unchanged. They can be applied directly to study endowment shocks in a neoclassical model. When intermediate goods are not traded or traded but their factor content is not reexported, as in Grossman and Rossi-Hansberg (2008), Propositions 2 and 3 can also be applied directly to the analysis of changes in trade costs. When the factor content of intermediate goods is reexported, as in Yi (2003), Propositions 2 and 3 can still be used, but they require the space of factors to be augmented. Specifically, one needs to treat factors that are imported directly and indirectly differently since they are subject to different (vectors of) iceberg trade costs.

#### IV. Identification

##### A. Econometric Model

In order to go from the economic model of Section IIA to an econometric model that can be estimated, we need to make additional assumptions on which variables are unobservable and which ones are not as well as the origins of the exogenous shocks generating the observable variables.

*Exogenous Shocks.*—Consider a dataset generated by the model of Section IIA at different dates indexed by  $t$ . At each point in time, we assume that preferences and technology in the original neoclassical trade model satisfy

$$(21) \quad u_{i,t}(\mathbf{q}_{i,t}) = \bar{u}_i(\{q_{ji,t}^k\}), \quad \text{for all } i,$$

$$(22) \quad f_{ji,t}^k(\mathbf{I}_{ji,t}^k) = \bar{f}_{ji}^k(\{I_{ji,t}^{nk}/\tau_{ji,t}^n\}), \quad \text{for all } i, j, \text{ and } k.$$

Factor endowments,  $\{v_{i,t}^n\}$ , and trade costs,  $\{\tau_{ji,t}^n\}$ , are allowed to vary over time, but utility and production functions,  $\{\bar{u}_i\}$  and  $\{\bar{f}_{ji}^k\}$ , are assumed to be constant.<sup>23</sup>

<sup>22</sup>Obviously, a solution to the previous maximization problem must always feature  $c_{jd}^k = 0$  for all  $d \neq i$  since country  $i$  cannot benefit from final consumption in other countries.

<sup>23</sup>It is possible to accommodate time-varying preference shocks that shift the relative value of all goods produced by a particular source country. They could be dealt with in the exact same way as we dealt with preference shocks in the reduced exchange model of Section IIIA. Note also that the absence of sector-specific productivity shocks is sufficient, but not necessary. What is crucial for the analysis below is that sector-specific productivity shocks do not affect the shape of factor demand. For example, if all goods enter symmetrically in the utility function, then a weaker sufficient condition is that the distribution of productivity across sectors is stable over time, though productivity in particular sectors may go up or down at particular points in time. Hanson, Lind, and Muendler (2014) offer empirical evidence consistent with that weaker condition.

In line with the analysis of Section III, equations (21) and (22) lead to the existence of a vector of effective factor prices,  $\omega_{i,t} \equiv \{w_{j,t}^n \tau_{ji,t}^n\}$ , such that factor demand in any country  $i$  and at any date  $t$  can be expressed as  $\chi_i(\omega_{i,t}, y_{i,t})$ .

*Observables and Unobservables.*—For any country  $i$  and for any date  $t$ , we assume that effective factor prices,  $\omega_{i,t} \equiv \{\omega_{ji,t}^n\}$ , are unobservable. Like in Section IIIA, we normalize the effective factor prices to 1 in all countries in some base period  $t_0$ :

$$(23) \quad \omega_{ji,t_0}^n = 1, \quad \text{for all } i, j, \text{ and } n.$$

This is the counterpart of equation (12). The only observables are: (i) factor expenditure shares,  $\mathbf{x}_{i,t} \equiv \{x_{ji,t}^n\}$ ; (ii) factor payments,  $\mathbf{y}_{i,t} \equiv \{y_{i,t}^n\}$ ; (iii) trade cost shifters,  $\mathbf{z}_{i,t}^\tau \equiv \{(z^\tau)_{ji,t}^n\}$ ; (iv) and an income shifter,  $z_{i,t}^y$ .

In principle, data on factor expenditure shares,  $\mathbf{x}_{i,t} \equiv \{x_{ji,t}^n\}$ , and factor payments,  $\mathbf{y}_{i,t} \equiv \{y_{i,t}^n\}$ , can be obtained from sources such as the World Input-Output Database. As already discussed in the introduction, a practical limitation of such datasets is that they implicitly assume that factor intensity is constant across destinations within the same industry. Since micro-level evidence, e.g., Bernard and Jensen (1999), suggests systematic variation in factor intensity between firms that serve domestic and foreign markets, one could potentially improve on the measurement of the factor content of trade by combining aggregate data from national accounts and firm-level data in a consistent way.<sup>24</sup> For the empirical application of Section V, we abstract from such considerations by assuming the existence of a composite factor in each country.<sup>25</sup> In this context, the total value of bilateral trade in goods is sufficient to compute factor expenditure shares.

We assume that trade cost shocks in the model,  $\tau_{ji,t}^n$ , are related to observable trade cost shifters in the data through

$$\ln \tau_{ji,t}^n = \ln (z^\tau)_{ji,t}^n + \varphi_{ji}^n + \tilde{\xi}_{j,t}^n + \eta_{ji,t}^n,$$

where  $\varphi_{ji}^n$  and  $\tilde{\xi}_{j,t}^n$  are exporter-importer-factor and exporter-factor-period specific components, respectively, and  $\eta_{ji,t}^n$  are idiosyncratic trade cost shocks. In Section V, we will use data on bilateral freight costs as trade cost shifters for (all) factors from a given destination. Combining the previous equation with the definition of effective factor prices,  $\omega_{ji,t}^n \equiv w_{j,t}^n \tau_{ji,t}^n$ , we then obtain

$$(24) \quad \ln \omega_{ji,t}^n = \ln (z^\tau)_{ji,t}^n + \varphi_{ji}^n + \xi_{j,t}^n + \eta_{ji,t}^n, \quad \text{for all } i, j, n, \text{ and } t,$$

<sup>24</sup>It should be clear that constructing factor expenditure shares,  $\mathbf{x}_{i,t}$ , in such a manner is simply an accounting exercise. It does not require structural estimation of production and consumption substitution across the whole world, as would be required, for instance, in factor content calculations that aim to identify the number of workers or hours that imports from a specific country have displaced. We note, however, that unless firm-level data record factor spending by destination, even such an approach would generate an imperfect measure of the true factor content of trade.

<sup>25</sup>In contrast, our focus on factor demand allows us to dispense with any restriction on the structure of the goods space. Since disaggregated data on both consumption and production are rarely available in practice, this is a nontrivial benefit of our approach. Compared to an empirical approach that would try to estimate demand and production functions over goods directly, we do not have to assume that goods can be aggregated into a relatively small set of industries.



with  $\xi_{j,t}^n \equiv \tilde{\xi}_{j,t}^n + \ln w_{j,t}^n$ . The second term,  $\varphi_{ji}^n$ , captures any source of trading frictions between country  $i$  and  $j$  that is stable over time. This includes usual proxies for trade costs like bilateral distance, whether  $i$  and  $j$  share a common language, or whether they have colonial ties: see, e.g., Anderson and van Wincoop (2004). Crucially, the third term,  $\xi_{j,t}^n$ , includes all variation in factor prices,  $w_{j,t}^n$ , which are the key endogenous variables in our model. Throughout our analysis, we impose the following exogeneity restriction.

**ASSUMPTION A1 (Exogeneity):**  $E[\eta_{ji,t}^n | \mathbf{z}_t] = 0$ , with  $\mathbf{z}_t \equiv \{\mathbf{z}_{i,t}^\tau, \mathbf{z}_{i,t}^\omega\}$  the vector of all instruments in period  $t$ .

Because of equation (24), A1 is stronger than assuming that relative trade cost shifters,  $\ln \mathbf{z}_{i,t}^\tau$ , can be used as instruments for effective factor prices,  $\ln \omega_{ji,t}^n$ , after controlling for all factors that are either exporter-importer-factor or exporter-factor-year specific. If we think of equation (24) as a first stage, it implies that reduced-form and IV estimates should coincide. Hence, we can infer the impact on factor demand of effective factor prices, which are not observable, by tracing out the impact of trade cost shifters, which are observable. Although the relationship to demand estimation is rarely made explicit, this is the same strategy used for the estimation of (constant) trade elasticities in the gravity literature where trade cost shifters are measured either as 1 plus the ad valorem bilateral tariff rate or as the ad valorem freight rate: see Head and Mayer (2014). In Section V, we will use data on bilateral freight costs as trade cost shifters for (all) factors from a given destination.<sup>26</sup>

Since effective factor prices,  $\omega_{ji,t}^n$ , are equal to the product of  $w_{j,t}^n$  and  $\tau_{ji,t}^n$ , an alternative would be to use measures of factor prices,  $w_{j,t}^n$ , as observable shifters of  $\omega_{ji,t}^n$ , instrumented, for instance, by population: see, e.g., Eaton and Kortum (2002) and Antràs, Fort, and Tintelnot (2016). Though this second approach would allow reduced-form and IV estimates to differ, we view the two approaches as very similar. Ultimately, whether the first or the second approach should be preferred boils down to asking: (i) whether effective factor prices are more likely to move one-for-one with proxies of iceberg trade costs, like freight costs, or with proxies of factor prices per efficiency unit, like those using wage data; and (ii) whether the exclusion restriction is more likely to be satisfied for freight costs (after controlling for exporter-importer-factor and exporter-factor-year fixed effects) than for population (after only controlling for the former fixed effects and observable country characteristics). The fact that freight costs, unlike wages, do not necessarily call for an instrument should not be viewed as a downside of our empirical strategy.

Following Newey and Powell (2003), we impose the following completeness condition.

<sup>26</sup> A common finding in the international macro literature is that exporters' cost shocks tend to be incompletely passed through into consumer prices: see, e.g., Burstein and Gopinath (2014). This observation does not by itself invalidate the aforementioned identification strategy. Within the context of a neoclassical model, such findings can be rationalized by assuming that foreign goods need to be distributed, which requires local factors of production, as in Burstein, Neves, and Rebelo (2003). In such a model, there is incomplete pass-through into consumer prices, as observed in the data, yet complete pass-through into effective factor prices, as assumed in equation (24).

ASSUMPTION A2 (Completeness): For any importer pair  $(i_1, i_2)$ , and any function  $g(\mathbf{x}_{i_1,t}, y_{i_1,t}, \mathbf{x}_{i_2,t}, y_{i_2,t})$  with finite expectation,  $E[g(\mathbf{x}_{i_1,t}, y_{i_1,t}, \mathbf{x}_{i_2,t}, y_{i_2,t}) | \mathbf{z}_t] = 0$  implies  $g(\mathbf{x}_{i_1,t}, y_{i_1,t}, \mathbf{x}_{i_2,t}, y_{i_2,t}) = 0$ .

Assumption A2 is the equivalent of a rank condition in the estimation of parametric models.<sup>27</sup>

### B. Identification of Invertible Demand Systems

We now establish that if the factor demand system is invertible, then factor prices and factor demand are identified under the assumptions of Section IVA. The argument follows the same steps as in Berry and Haile (2014). The next subsection will offer sufficient conditions under which invertibility holds.

Consider the following restriction on the factor demand system.

ASSUMPTION A3 (Invertibility): In any country  $i$ , for any observed expenditure shares,  $\mathbf{x} > \mathbf{0}$ , and any observed income level,  $y > 0$ , there exists a unique vector of relative effective factor prices,  $(\chi_i)^{-1}(\mathbf{x}, y)$ , such that all  $\omega_i$  satisfying  $\mathbf{x} \in \chi_i(\omega_i, y)$  also satisfy  $\omega_{ji}^n/\omega_{1i}^1 = (\chi_{ji}^n)^{-1}(\mathbf{x}, y)$ .

Take an equilibrium vector of effective factor prices,  $\omega_{i,t}$ , in some country  $i$  at date  $t$ . By Assumption A3, we can express the vector of relative effective factor prices as a function of the vector of market shares and income,

$$(25) \quad \omega_{ji,t}^n/\omega_{1i,t}^1 = (\chi_{ji}^n)^{-1}(\mathbf{x}_{i,t}, y_{i,t}).$$

Taking logs and using equation (24), we then have

$$\Delta \eta_{ji,t}^n = \ln(\chi_{ji}^n)^{-1}(\mathbf{x}_{i,t}, y_{i,t}) - \Delta \ln(z^\tau)_{ji,t}^n - \Delta \varphi_{ji}^n - \Delta \xi_{j,t}^n,$$

where  $\Delta$  denotes differences relative to factor 1 in country 1, e.g.,  $\Delta \eta_{ji,t}^n \equiv \eta_{ji,t}^n - \eta_{1i,t}^1$ . And taking a second difference between an arbitrary pair of importers,  $i_1$  and  $i_2$ , in order to eliminate the exporter-factor-period specific component, we obtain

$$\begin{aligned} \Delta \eta_{j_1 i_1, t}^n - \Delta \eta_{j_2 i_2, t}^n &= \ln(\chi_{j_1 i_1}^n)^{-1}(\mathbf{x}_{i_1, t}, y_{i_1, t}) - \ln(\chi_{j_2 i_2}^n)^{-1}(\mathbf{x}_{i_2, t}, y_{i_2, t}) \\ &\quad - (\Delta \ln(z^\tau)_{j_1 i_1, t}^n - \Delta \ln(z^\tau)_{j_2 i_2, t}^n) - (\Delta \varphi_{j_1}^n - \Delta \varphi_{j_2}^n). \end{aligned}$$

<sup>27</sup> Going from a finite to an infinite dimensional space of parameters leads to nontrivial issues. Newey (2013, p. 552) notes that: "In fully nonparametric models (that are infinite dimensional), completeness is not testable, as pointed out by Canay, Santos, and Shaikh (2013). In these models the reduced form is like an infinite dimensional matrix with eigenvalues that have a limit point at zero. Nonidentification occurs when at least one of the eigenvalues equals zero. The problem with testing this hypothesis is that one cannot distinguish empirically a model with a zero eigenvalue from one where the eigenvalues have a limit point of zero. However, completeness is generic." We have little to add to this discussion.

Under Assumption A1, this leads to the following moment condition:

$$\begin{aligned} E[\ln(\chi_{j_1}^n)^{-1}(\mathbf{x}_{i_1,t}, y_{i_1,t}) - \ln(\chi_{j_2}^n)^{-1}(\mathbf{x}_{i_2,t}, y_{i_2,t}) - \zeta_{j_1 i_2}^n | \mathbf{z}_t] \\ = \Delta \ln(z^\tau)_{j_1,t}^n - \Delta \ln(z^\tau)_{j_2,t}^n, \end{aligned}$$

with the constant  $\zeta_{j_1 i_2}^n \equiv \Delta \varphi_{j_1}^n - \Delta \varphi_{j_2}^n$ .

Now suppose that there exist  $((\chi_{j_1}^n)^{-1}, (\chi_{j_2}^n)^{-1}, \zeta_{j_1 i_2}^n)$  and  $((\tilde{\chi}_{j_1}^n)^{-1}, (\tilde{\chi}_{j_2}^n)^{-1}, \tilde{\zeta}_{j_1 i_2}^n)$  such that the previous moment condition holds. Then, we must have

$$\begin{aligned} E[\ln(\chi_{j_1}^n)^{-1}(\mathbf{x}_{i_1,t}, y_{i_1,t}) - \ln(\tilde{\chi}_{j_1}^n)^{-1}(\mathbf{x}_{i_1,t}, y_{i_1,t}) - \ln(\chi_{j_2}^n)^{-1}(\mathbf{x}_{i_2,t}, y_{i_2,t}) \\ + \ln(\tilde{\chi}_{j_2}^n)^{-1}(\mathbf{x}_{i_2,t}, y_{i_2,t}) - \zeta_{j_1 i_2}^n + \tilde{\zeta}_{j_1 i_2}^n | \mathbf{z}_t] = 0. \end{aligned}$$

Under Assumption A2, this requires

$$\begin{aligned} \ln(\chi_{j_1}^n)^{-1}(\mathbf{x}_{i_1,t}, y_{i_1,t}) - \ln(\tilde{\chi}_{j_1}^n)^{-1}(\mathbf{x}_{i_1,t}, y_{i_1,t}) \\ = \ln(\chi_{j_2}^n)^{-1}(\mathbf{x}_{i_2,t}, y_{i_2,t}) - \ln(\tilde{\chi}_{j_2}^n)^{-1}(\mathbf{x}_{i_2,t}, y_{i_2,t}) + \zeta_{j_1 i_2}^n - \tilde{\zeta}_{j_1 i_2}^n, \end{aligned}$$

for all  $(\mathbf{x}_{i_1,t}, y_{i_1,t}, \mathbf{x}_{i_2,t}, y_{i_2,t})$ . Since the right-hand side of the previous equation does not vary with  $(\mathbf{x}_{i_1,t}, y_{i_1,t})$ , the left-hand side cannot vary with  $(\mathbf{x}_{i_1,t}, y_{i_1,t})$  either. This establishes that  $(\chi_{j_1}^n)^{-1}$  is equal to  $(\tilde{\chi}_{j_1}^n)^{-1}$  up to a constant. Furthermore, for the normalization (23) to hold, we must have  $(\chi_{j_1}^n)^{-1}(\mathbf{x}_{i_1,t_0}, y_{i_1,t_0}) = (\tilde{\chi}_{j_1}^n)^{-1}(\mathbf{x}_{i_1,t_0}, y_{i_1,t_0}) = 1$ , which establishes that the previous constant is zero. We conclude that having normalized effective factor prices in the base period,  $(\chi_{j_1}^n)^{-1}$  is identified. The same argument establishes the identification of  $(\chi_{j_2}^n)^{-1}$ .

Repeating the previous argument for all exporters  $j$  and all factors  $n$ , we obtain that for any importing country  $i$ , the inverse factor demand,  $(\chi_i)^{-1}$ , is identified. Relative effective factor prices are then uniquely determined by equation (25). Finally, given data on factor expenditure shares,  $\mathbf{x}_{i,t}$ , and knowledge of the relative effective factor prices, the factor demand system,  $\chi_i$ , is identified as well.

We summarize the previous discussion in the next proposition.

**PROPOSITION 4:** *Suppose that Assumptions A1–A3 hold. Then factor demand and relative effective factor prices are identified.*

### C. Ricardian Example

The invertibility of demand plays a key role in Proposition 4. We now provide sufficient conditions on the primitives of a neoclassical trade model such that Assumption A3 holds. We also show that under the same conditions, a competitive equilibrium is unique. Hence, counterfactual changes in factor prices and welfare are also nonparametrically identified in this environment. We will come back to the same environment for our empirical application in Sections V and VI.

Consider an economy in which utility and production functions satisfy

$$(26) \quad u_i(\mathbf{q}_i) = \bar{u}_i \left( \left\{ \sum_j q_{ji}^k \right\} \right), \quad \text{for all } i,$$

$$(27) \quad f_{ji}^k(\mathbf{I}_{ji}^k) = \alpha_{ji}^k \bar{f}_j(\mathbf{I}_{ji}^k) / \tau_{ji}, \quad \text{for all } i, j, \text{ and } k,$$

where  $\bar{u}_i$  is a homothetic utility function that satisfies standard Inada conditions;  $\alpha_{ji}^k$  is total factor productivity in country  $j$  and sector  $k$  when selling to country  $i$ ;  $\bar{f}_j$  is a production function, common to all sectors and destinations; and  $\tau_{ji}$  is a bilateral iceberg trade cost. Given equation (26), the Inada conditions are imposed to rule out zero expenditure shares on all goods.<sup>28</sup> The crucial restriction is imposed in equation (27). It states that all goods from country  $j$  use factors with the same intensity. Hence, everything is as if there was only one factor per country with price  $c_j \equiv \min_i \left\{ \sum w_j^n \tilde{l}_j^n \mid \bar{f}_j(\mathbf{I}) = 1 \right\}$  and endowment  $\bar{f}_j(\mathbf{v}_j)$ .

In light of the previous discussion, we refer to an economy that satisfies (26) and (27) as a Ricardian economy. In such an environment, homotheticity and no differences in factor intensity imply that we can write the demand for factors in country  $i$  as  $\chi_i(\omega_i)$ , with  $\omega_i \equiv \{\tau_{ji}c_j\}$  the vector of effective prices for the composite factors.

As discussed in Berry, Gandhi, and Haile (2013), a sufficient condition for a demand function to be invertible over its support is that it satisfies the connected substitutes property.<sup>29</sup> This property has a long tradition in general equilibrium theory where it is used to establish the uniqueness of competitive equilibrium prices, through the injectivity of the excess demand function: see Arrow and Hahn (1971, p. 227). For the purposes of this paper, we need a slightly more general version of this property that applies to demand correspondences, not just functions. We focus on the following generalization adapted from Howitt (1980).

**DEFINITION 3 (Connected Substitutes):** *A correspondence  $\chi : \mathbb{R}_{++}^m \rightarrow P(\mathbb{R}_{++}^m)$  satisfies the connected substitutes property if for any  $\omega$  and  $\omega' \in \mathbb{R}_{++}^m$ , any  $\mathbf{x} \in \chi(\omega)$ , any  $\mathbf{x}' \in \chi(\omega')$ , and any nontrivial partition  $\{M_1, M_2\}$  of  $M \equiv \{1, \dots, m\}$ ,  $\omega'_j > \omega_j$  for all  $j \in M_1$  and  $\omega'_j = \omega_j$  for all  $j \in M_2$  imply  $\sum_{j \in M_2} x'_j > \sum_{j \in M_2} x_j$ .*

Our first lemma provides sufficient conditions under which the factor demand system of a Ricardian economy is invertible over its support.

<sup>28</sup>By itself, the assumption that goods from different exporting countries are perfect substitutes, as described in equation (26), is without loss of generality. To see this, note that the Armington model corresponds to the limit case in which each good  $k$  can only be produced in only one country. We only impose equation (26) to weaken the Inada conditions. Namely, we require all countries to consume all goods, not all goods from all origins.

<sup>29</sup>If we were able to observe the quantities of factor services demanded by each country directly, rather than factor expenditure shares, invertibility would be a straightforward issue in the context of this paper. From Proposition 1, we know that there must be a representative agent whose factor demand solves (9). Whenever the reduced utility function is differentiable at the optimum, the first-order conditions of the utility maximization problem (9) immediately imply that factor prices are determined (up to a normalization) by the gradient of the reduced utility function, evaluated at the optimal quantities of factor demanded. The case of Cobb-Douglas utility is an extreme example that shows that the previous argument does not carry over to expenditure shares. In that case, there is uniqueness of prices conditional on quantities demanded, but not conditional on expenditure shares.

LEMMA 1: *Consider a Ricardian economy. If good expenditure shares satisfy the connected substitutes property, then for any vector of factor expenditure shares,  $\mathbf{x} > 0$ , there is at most one vector (up to a normalization) of effective factor prices,  $\omega$ , such that  $\mathbf{x} \in \chi_i(\omega)$ .*

The formal proof can be found in Appendix A. The general strategy is similar to the one used by Scarf and Wilson (2005) to establish the uniqueness of competitive equilibria in a Ricardian model. The key idea is to show that if expenditure shares on goods satisfy the connected substitutes property, then the expenditure shares on factors must satisfy the same property. At that point, the invertibility of the factor demand system follows from standard arguments: see, e.g., Proposition 17.F.3 in Mas-Colell, Whinston, and Green (1995). The only minor technicality is that the demand function may be a correspondence, which Definition 3 is designed to address.

In light of the discussion above, it should not be surprising that the same sufficient conditions lead to the uniqueness of the competitive equilibrium.

LEMMA 2: *Consider a Ricardian economy. If good expenditure shares satisfy the connected substitutes property, then the vector of equilibrium factor prices,  $(c_1, \dots, c_I)$ , is unique (up to a normalization).*

Let us take stock. Proposition 4 and Lemma 1 imply that factor demand is nonparametrically identified in a Ricardian economy if Assumption A1 and Assumption A2 hold and good expenditure shares satisfy the connected substitutes property. Since all the assumptions of Section III are satisfied, Proposition 2, Proposition 3, and Lemma 2 further imply that proportional changes in factor prices and welfare are uniquely determined given data on initial expenditure shares and factor payments,  $\{x_{ji}^n\}$  and  $\{y_i^n\}$ , and an estimate of factor demand,  $\chi_i$ .<sup>30</sup> This leads to our final observation.

COROLLARY 2: *Consider a Ricardian economy. If Assumptions A1 and A2 hold and good expenditure shares satisfy the connected substitutes property, then proportional changes in factor prices and welfare caused by trade cost shocks and endowment shocks are nonparametrically identified.*

## V. Estimation

The results above highlight two important features of neoclassical trade models. First, counterfactual changes in trade costs and factor endowments can be studied with only the knowledge of a reduced factor demand system. Second, this reduced demand system can be nonparametrically identified from standard data sources on international trade in goods and standard exclusion restrictions. Armed with these theoretical results we now turn to a strategy for estimating the reduced demand system, in practice.

<sup>30</sup>Proportional changes in the factor content of trade are also unique if factor demand,  $\chi_i$ , is single-valued at the initial and counterfactual equilibria.

### A. From Asymptopia to Mixed CES

Nonparametric identification results, like those presented in Section IV, are asymptotic in nature. They answer the question of whether one could point identify each of the potentially infinite-dimensional parameters of a model with a dataset whose sample size tends to infinity—formally, whether there exists a unique mapping from population data to model parameters. As noted by Chiappori and Ekeland (2009), such results are useful because they can help select the most adequate moment conditions, that is, the source of variation in the data directly related to the economic relation of interest.

Of course, datasets in the real world often feature a small number of observations and little exogenous variation. So estimation must inevitably proceed parametrically. Our goal here is to do so in a flexible manner, drawing on recent advances in the area of applied demand estimation: see, e.g., Nevo (2011). In the spirit of dimensionality-reduction, we start by making three assumptions. We assume that: (i) preferences are homothetic, so that we can ignore the effect of income on expenditure shares; (ii) all goods have the same factor intensity in each country, so that we can focus on a single composite factor per country (and hence drop the  $n$  superscript in what follows); and (iii) cross-country differences in factor demand can be reduced to differences in time-varying effective factor prices and time-invariant shifters,  $\chi_i(\omega_{i,t}) = \chi(\{\mu_{ji}\omega_{ji,t}\})$  for all importers  $i$ , so that we can use both time series and cross-country variation to estimate  $\chi$ . These assumptions are restrictive, but all are standard in the existing gravity literature.<sup>31</sup>

Since there is one composite factor in each country, we drop superscripts  $n$  from now on. For importer  $i$  in year  $t$ ,  $\omega_{ji,t}$  is the effective price of the composite factor from country  $j$ , and  $\omega_{i,t} \equiv \{\omega_{ji,t}\}$  is the associated vector of effective prices. Taking inspiration from Berry (1994) and Berry, Levinsohn, and Pakes (1995), we posit that the expenditure share that country  $i$  devotes to the factor from country  $j$  in year  $t$  can be expressed as

$$(28) \quad \chi_{ji}(\omega_{i,t}) = \int \frac{(\kappa_j)^{\sigma_\alpha \alpha} (\mu_{ji} \omega_{ji,t})^{-(\bar{\epsilon} \cdot \epsilon^{\sigma_\epsilon})}}{\sum_{l=1}^N (\kappa_l)^{\sigma_\alpha \alpha} (\mu_{li} \omega_{li,t})^{-(\bar{\epsilon} \cdot \epsilon^{\sigma_\epsilon})}} dF(\alpha, \epsilon),$$

where  $\kappa \equiv \{\kappa_j\}$  is a vector of observable exporter characteristics,  $\mu_i \equiv \{\mu_{ji}\}$  is a vector of unobserved importer-exporter shifters, and  $\{\bar{\epsilon}, \sigma_\alpha, \sigma_\epsilon\}$  are the structural parameters of interest. The random draws  $(\alpha, \epsilon)$  can be interpreted as unobserved heterogeneity across goods in the elasticities with respect to effective factor prices,  $\omega_{ji,t}$ , and exporter characteristic,  $\kappa_j$ . We come back to this point below.

<sup>31</sup>Fajgelbaum and Khandelwal (2016) recently introduced nonhomothetic preferences to study how gains from trade vary across income groups. As discussed below, our dataset only includes two importing countries: the United States and Australia. So, there is very little variation that we can use to estimate nonhomotheticities. Similarly, introducing differences in factor intensity across sectors would further require estimates of the extent to which multiple factors are substitutable for one another within each country. While in principle this can be achieved with supply-side shifters of relative factor prices, finding such shifters in practice has proven difficult: see, e.g., Oberfield and Raval (2014) for a recent discussion of the capital-labor case.



In our baseline analysis, we assume that  $\kappa_j$  is the per capita GDP of country  $j$  relative to the per capita GDP of the United States ( $j = 1$ ) in the presample period.<sup>32</sup> We also assume that the joint distribution  $F(\alpha, \epsilon)$  is such that  $\alpha$  and  $\ln \epsilon$  have a joint standard normal distribution with an identity covariance matrix.<sup>33</sup> Thus, the demand system is completely characterized by three structural parameters,  $\{\bar{\epsilon}, \sigma_\alpha, \sigma_\epsilon\}$ , with the importer-specific shifters,  $\mu_i$ , merely pinned down by the normalization of effective factor prices in the base period.<sup>34</sup>

This particular functional form is attractive for three reasons. First, it nests the case of CES demand. That is, in the special case of  $\sigma_\alpha = \sigma_\epsilon = 0$ , we recover a standard gravity model with trade elasticity  $\bar{\epsilon}$ . When  $\sigma_\alpha \neq 0$  or  $\sigma_\epsilon \neq 0$ , the demand system in equation (28) becomes a random coefficients version of CES demand, in the same way that the mixed logit demand system in Berry, Levinsohn, and Pakes (1995) is a random coefficients version of logit demand. For this reason, we refer to our demand system as *mixed CES*.

Second, the demand system in equation (28) is invertible: any CES demand satisfies the connected substitutes property, provided that  $\bar{\epsilon}$  is different from zero, and the sum of demand functions that satisfy the connected substitutes property must also satisfy this property. This implies that the nonparametric identification results of Section IV continue to hold.

Third, the mixed CES demand system captures flexibly and parsimoniously a number of natural features of demand substitution patterns through the structural parameters  $\sigma_\alpha$  and  $\sigma_\epsilon$ . To see this, define the share of the factor from country  $j$  in expenditures of country  $i$  conditional on  $(\alpha, \epsilon)$ :

$$(29) \quad x_{ji,t}(\alpha, \epsilon) \equiv \frac{(\kappa_j)^{\sigma_\alpha} (\mu_{ji} \omega_{ji,t})^{-(\bar{\epsilon} \cdot \epsilon^{\sigma_\epsilon})}}{\sum_{l=1}^N (\kappa_l)^{\sigma_\alpha} (\mu_{li} \omega_{li,t})^{-(\bar{\epsilon} \cdot \epsilon^{\sigma_\epsilon})}}.$$

Now take three exporter countries  $j, l$ , and  $r$  competing in the same importing market  $i$  in year  $t$ . Consider how the demand for the factor from country  $j$  relative to the factor from the reference country  $r$  depends on the effective price of the factor from country  $l$  relative to that of country  $r$ . This cross-price elasticity of relative demand shares to relative prices is given by

$$(30) \quad \frac{\partial \ln \left( \frac{\chi_{ji}(\omega_{i,t})}{\chi_{ri}(\omega_{i,t})} \right)}{\partial \ln \left( \frac{\omega_{li,t}}{\omega_{ri,t}} \right)} = \int (\bar{\epsilon} \cdot \epsilon^{\sigma_\epsilon}) \left( \frac{x_{ji,t}(\alpha, \epsilon)}{\chi_{ji}(\omega_{i,t})} - \frac{x_{ri,t}(\alpha, \epsilon)}{\chi_{ri}(\omega_{i,t})} \right) x_{li,t}(\alpha, \epsilon) dF(\alpha, \epsilon).$$

<sup>32</sup>More generally, one could incorporate a multivariate set of time-varying characteristics by setting  $\kappa_{j,t} \equiv \gamma \cdot \mathbf{u}_{j,t}$  where  $\mathbf{u}_{j,t}$  is a vector of characteristics for exporter  $j$  at year  $t$  and  $\gamma$  is the parameter vector that intermediates the effect of these characteristics on market shares. An alternative modeling strategy would be to organize countries into groups, based on some observed characteristic, and then estimate a nested CES system across countries. This would be analogous to the nested logit approach in Goldberg (1995).

<sup>33</sup>We incorporate the heterogeneity in  $\epsilon$  with a positive multiplicative shifter to guarantee no sign variation in the trade elasticity. In other words, the sign of the trade elasticity is entirely determined by  $\bar{\epsilon}$  but its magnitude is affected by the multiplicative shifter,  $\epsilon^{\sigma_\epsilon}$ , whose distribution is log normal with mean zero and variance  $\sigma_\epsilon$ .

<sup>34</sup>Specifically, conditional on  $\{\bar{\epsilon}, \sigma_\alpha, \sigma_\epsilon\}$ , the vector of shifters  $\mu_i$  is given by any solution to

$$x_{ji,t_0} = \int \frac{(\kappa_j)^{\sigma_\alpha} (\mu_{ji})^{-(\bar{\epsilon} \cdot \epsilon^{\sigma_\epsilon})}}{\sum_{l=1}^N (\kappa_l)^{\sigma_\alpha} (\mu_{li})^{-(\bar{\epsilon} \cdot \epsilon^{\sigma_\epsilon})}} dF(\alpha, \epsilon).$$

This expression highlights key features of the demand system in equation (28). As expected, setting  $\sigma_\alpha = \sigma_\epsilon = 0$  recovers the well-known property of independence of irrelevant alternatives (IIA) embedded in the CES demand system: the cross-price elasticity is zero.<sup>35</sup> Departures from this special case yield richer patterns of substitution. The cross-price elasticity is relatively larger when  $x_{ji,t}(\alpha, \epsilon)$  and  $x_{li,t}(\alpha, \epsilon)$  co-move more than  $x_{ri,t}(\alpha, \epsilon)$  and  $x_{li,t}(\alpha, \epsilon)$  in the  $(\alpha, \epsilon)$  space. From equation (29), we can see that such a pattern is generated by two channels. Whenever  $\sigma_\alpha \neq 0$  and  $\sigma_\epsilon = 0$ , this is the case if countries  $j$  and  $l$  are more similar in terms of their characteristics,  $\kappa$ , than countries  $r$  and  $l$  are (i.e.,  $|\kappa_j - \kappa_l| < |\kappa_r - \kappa_l|$ ). Alternatively, whenever  $\sigma_\alpha = 0$  and  $\sigma_\epsilon \neq 0$ , this pattern occurs if countries  $j$  and  $l$  are more similar in terms of their effective factor price than countries  $r$  and  $l$  are—this is then intrinsically related to market shares (i.e.,  $|\chi_{ji(\omega_{i,t})} - \chi_{li(\omega_{i,t})}| < |\chi_{ri(\omega_{i,t})} - \chi_{li(\omega_{i,t})}|$ ).

One particular set of microfoundations that would lead to the factor demand system in equation (28) is that stemming from: (i) a Cobb-Douglas utility with equal weights over a continuum of sectors, with a lower-level CES nest over a continuum of varieties in each sector; and (ii) country-and-sector-specific Fréchet distributions of productivity across varieties (with common shape parameters across countries). Under this interpretation, each sector is fully characterized by its corresponding pair  $(\alpha, \epsilon)$ , with  $F(\alpha, \epsilon)$  representing the distribution of sector attributes. In this sense, the factor demand system in equation (28) is closely related to the nested CES demand implied by standard multisector models in the field: see, e.g., Costinot, Donaldson, and Komunjer (2012) and Caliendo and Parro (2015).<sup>36</sup>

Rather than the specific functional forms that we focus on, the key difference between our approach, based on mixed CES, and existing approaches in the field, based on multisector gravity models, concerns the source of variation used. The results in Section IV demonstrate that the aggregate factor demand system—which, as we have argued, is all that is required to study the counterfactual scenarios we consider here—is nonparametrically identified from aggregate data on factor spending shares. This is the variation that we will use next. Multisector models, in contrast, are estimated using within-sector variation. And while sector-level factor demand relations are identified with sector-level data, the aggregate factor demand function, along with its essential aggregate cross-price elasticities, is not.

To see the potential importance of this distinction, consider an economy in which the true factor demand system is CES, with trade elasticity  $\bar{\epsilon}$ . In that case, a researcher using sector-level data would recover the true lower-level elasticity of substitution across countries within each sector, i.e.,  $\bar{\epsilon}$ . However, positing a nested-CES utility function with an upper-level Cobb-Douglas aggregator, the same researcher would wrongly conclude that the upper-level elasticity between sectors is equal to 1 rather than  $\bar{\epsilon}$ . In contrast, in the context of this simple example, a researcher using

<sup>35</sup>This follows immediately from the observation that  $x_{ji,t}(\alpha, \epsilon) = \chi_{ji(\omega_{i,t})}$  for all  $j$  if  $\sigma_\alpha = \sigma_\epsilon = 0$ . Also, it is straightforward to verify that, in this case, the own-price elasticity is constant and equal to  $-\bar{\epsilon}$ .

<sup>36</sup>The previous assumptions are sufficient, but not necessary. Under the assumption of Fréchet distributions, for instance, the assumption of a lower-level CES utility could be relaxed to allow for any symmetric utility function across varieties. Similarly, under the assumption of nested CES utility, one could obtain the same factor demand system by assuming an Armington model, as in Anderson and Yotov (2010).

aggregate data and assuming a mixed CES demand system would rightly conclude that factor demand is CES.<sup>37</sup>

Summarizing the discussion above, the mixed CES demand in equation (28) not only nests commonly used functional forms in the literature but also captures in a parsimonious manner the natural feature that factors similar in the  $\kappa$ -space are closer substitutes.<sup>38</sup> Given the essential role played by these cross-price elasticities of substitution in many counterfactual scenarios of interest, we consider of paramount importance the ability of an estimator to let the data speak directly to these phenomena.

### B. Estimation Procedure

We now turn to the estimation of the structural parameters  $\{\bar{\epsilon}, \sigma_\alpha, \sigma_\epsilon\}$  in equation (28). Building on the identification result of Section IV, the estimator is based on the existence of an observed and exogenous component of effective factor prices. Later, we take this cost shifter,  $z_{ji}^\tau$ , to be the reported freight charges between trading partners.

Our estimation procedure follows closely the methodology developed by Berry, Levinsohn, and Pakes (1995). Since the mixed CES demand system is invertible, the same steps as in Section IVB imply the following (cross-sectional) difference-in-differences,

$$\begin{aligned} \Delta \eta_{ji,t} - \Delta \eta_{j1,t} &= \ln(\chi_{ji})^{-1}(\mathbf{x}_{i,t}) - \ln(\chi_{j1})^{-1}(\mathbf{x}_{1,t}) \\ &\quad - (\Delta \ln(z^\tau)_{ji,t} - \Delta \ln(z^\tau)_{j1,t}) - (\Delta \varphi_{ji} - \Delta \varphi_{j1}), \end{aligned}$$

where country 1 (which we take to be the United States) is the reference country in both the first- and second-differences, e.g.,  $\Delta \eta_{ji,t} \equiv \eta_{ji,t} - \eta_{1i,t}$ . Using the fact that factor demand systems are invariant across countries up to time invariant shifters,  $\chi_i(\omega_{i,t}) = \chi(\{\mu_{ji}\omega_{ji,t}\})$ , this further implies

(31)

$$\Delta \eta_{ji,t} - \Delta \eta_{j1,t} = \ln \chi_j^{-1}(\mathbf{x}_{i,t}) - \ln \chi_j^{-1}(\mathbf{x}_{1,t}) - (\Delta \ln(z^\tau)_{ji,t} - \Delta \ln(z^\tau)_{j1,t}) + \zeta_{ji},$$

with

$$\zeta_{ji} \equiv -(\Delta \varphi_{ji} - \Delta \varphi_{j1}) - (\Delta \ln \mu_{ji} - \Delta \ln \mu_{j1}).$$

<sup>37</sup>Of course, when using multisector gravity models, one could relax the assumption that the aggregator is Cobb-Douglas and attempt to estimate directly the aggregate demand for the sectoral composite goods. But at that point, given the dimensionality of the demand system across goods that needs to be estimated, it is not clear what the benefit is compared to estimating the factor demand system directly. Exploring the quantitative implications of using these two different approaches, under various assumptions about the true demand system, is an interesting topic for future research.

<sup>38</sup>The translog demand system—as used in the Armington context by Novy (2013)—is an important exception not covered by the demand system in (28). One way to nest both CES and translog would be to use the CES-translog demand system introduced by Pollak, Sickles, and Wales (1984). While it is attractive to consider a demand system that nests both CES and translog, the main difficulty with using such a system in our setting is designing moment conditions that directly relate to the nonlinear parameters of this extended CES-translog system. One advantage of the mixed CES system is the clear connection between parameters and the structure of cross-price elasticities. As discussed below, this provides guidance for the choice of moment conditions.

Now consider the structural residual,

$$e_{ji,t}(\boldsymbol{\theta}) \equiv \ln \chi_j^{-1}(\mathbf{x}_{i,t}) - \ln \chi_j^{-1}(\mathbf{x}_{1,t}) - (\Delta \ln(z^\tau)_{ji,t} - \Delta \ln(z^\tau)_{j1,t}) + \zeta_{ji},$$

which is a function of the structural parameters,  $\boldsymbol{\theta} \equiv (\sigma_\alpha, \sigma_\epsilon, \bar{\epsilon}, \{\zeta_{ji}\})$ . Given a vector of instruments,  $\mathbf{Z}_{ji,t}$ , that satisfies the following moment conditions:

$$E((\Delta \eta_{ji,t} - \Delta \eta_{j1,t}) \mathbf{Z}_{ji,t}) = 0,$$

we can construct a consistent GMM estimator of  $\boldsymbol{\theta}$  by solving for

$$(32) \quad \hat{\boldsymbol{\theta}} = \arg \min_{\boldsymbol{\theta}} \mathbf{e}(\boldsymbol{\theta})' \mathbf{Z} \Phi \mathbf{Z}' \mathbf{e}(\boldsymbol{\theta}),$$

where  $\Phi$  is a matrix of moment weights. The details of the estimation procedure can be found in Appendix B.

To build instruments for the estimation of  $\boldsymbol{\theta}$ , we rely on the exogeneity restriction described in Assumption A1. Since A1 holds for any exporter-importer pair,  $(\Delta \eta_{ji,t} - \Delta \eta_{j1,t})$  must be uncorrelated with any function of trade cost shifters in period  $t$  as well as with any export-importer dummy. Our first set of instruments consists of an exporter's own trade costs shifter,  $\Delta \ln(z^\tau)_{ji,t} - \Delta \ln(z^\tau)_{j1,t}$ , as well as a full vector of exporter-importer dummies, which we denote by  $\mathbf{d}_{ji,t}$ . This is the usual set of regressors included in the estimation of gravity equations.<sup>39</sup> Our second set of instruments focuses on the trade cost shifters of an exporter's competitors,  $\{\Delta \ln(z^\tau)_{li,t}\}$ . Following the intuition for the IIA violation implied by  $(\sigma_\alpha, \sigma_\epsilon)$ , we propose additional instruments for exporter  $j$  that are based on the interaction between the trade cost of competitors,  $z_{li,t}^\tau$ , and their per capita GDP difference,  $|\kappa_j - \kappa_l|$ . Specifically, we use as instruments  $|\kappa_j - \kappa_l|(\ln z_{li,t}^\tau - \ln z_{l1,t}^\tau)$  for all  $l$ . Intuitively, this choice of instruments is designed to explore the extent to which distance in the characteristic space,  $|\kappa_j - \kappa_l|$ , affects cross-price elasticities. The final instrument vector combines these two components:  $\mathbf{Z}_{ji,t} \equiv (\Delta \ln(z^\tau)_{ji,t} - \Delta \ln(z^\tau)_{j1,t}, \{|\kappa_j - \kappa_l|(\ln z_{li,t}^\tau - \ln z_{l1,t}^\tau)\}, \mathbf{d}_{ji,t})$ .

While data requirements for the construction of our instruments are nontrivial, they are far less demanding than what would be required if one wanted to apply methods from industrial organization directly to the structural estimation of demand for goods. When using such methods, it is typical to focus on a narrow class of goods, like automobiles or ready-to-eat cereals. If one wanted to follow the exact same strategy in a general equilibrium context, one would need the same type of instruments within each narrowly defined goods class. Instead, we propose to focus on the estimation of the factor demand system whose macro-elasticities already contain all the information required (for the counterfactual questions of interest here) about the previous micro-elasticities.

<sup>39</sup>One should think of equation (31) as the difference-in-differences version of a gravity equation, that corresponds to the special case  $(\chi_j)^{-1}(\mathbf{x}_{i,t}) = (x_{ji,t}/x_{1i,t})^{-1/\bar{\epsilon}}$ , generalized to a mixed CES demand system. This explains why the exporter-period and importer-period fixed effects that would traditionally be included in the gravity literature, controls for the country sizes and so-called multilateral resistance terms, do not appear.

### C. Data

As described above, our estimation procedure draws on three types of data: (i) data on the total value of bilateral trade in goods, which can then be converted into expenditure shares, denoted by  $x_{ji,t}$ ; (ii) data on bilateral freight costs, denoted by  $z_{ji,t}^{\tau}$ ; and (iii) data on per capita GDP, denoted by  $\kappa_j$ . In addition, our counterfactual procedure requires data on (iv) total income by country, denoted by  $y_{j,t}$ .

We obtain data on  $x_{ji,t}$  and  $y_{j,t}$  from the World Input-Output Database for all years between 1995 and 2011 (Timmer et al. 2015). Following Shapiro (2016), data on  $z_{ji,t}^{\tau}$  are available from the publicly available import data for two importers  $i$ , Australia and the United States, in all years  $t$  from 1990 to 2010.<sup>40</sup> To avoid the possibility of zero trade flows, we focus on the 36 largest exporters to Australia and the United States, and aggregate all other countries up to a single Rest of World unit. In the estimation of  $\theta$ , we use all years with available information on trade flows and freight costs, 1995–2010. Finally, we obtain the information on per capita GDP necessary to construct  $\kappa_j$  from the Penn World Table, version 8.0 (Feenstra, Inklaar, and Timmer 2015).<sup>41</sup> The list of exporters along with their per capita GDP values is presented on Table A1 in Appendix C.

### D. Estimation Results

*Reduced-Form Evidence.*—Before turning to our estimates of the structural parameters, we begin with a simpler approach that builds directly on the standard gravity model. Our goal is twofold. First, we illustrate that the deviations from IIA motivated in Section VA are a systematic feature of the data. Second, we document that these deviations are directly related to the similarity of competitors in terms of per capita GDP. To this end, we estimate the following equation:

$$(33) \quad \Delta \ln(x_{jAUS,t}) - \Delta \ln(x_{jUS,t}) = \bar{\epsilon}(\Delta \ln z_{jAUS,t}^{\tau} - \Delta \ln z_{jUS,t}^{\tau}) \\ + \sum_l \gamma_l (|\kappa_j - \kappa_l| (\ln z_{jAUS,t}^{\tau} - \ln z_{jUS,t}^{\tau})) + \zeta_j + \eta_{j,t},$$

where  $x_{ji,t}$  is the share of country  $j$  exports in the expenditures of country  $i = \{AUS, US\}$  at year  $t$ ,  $z_{ji,t}^{\tau}$  is the bilateral freight cost from country  $j$  to country  $i$  at year  $t$ ,  $\zeta_j$  is an exporter fixed effect, and, as before, the  $\Delta$  operator takes the difference relative to one exporter, which we take to be the United States.

The IIA property implies that in any importing country, other competitors' costs have no effect on the demand for goods from exporter  $j$  relative to the reference exporter. In specification (33), the IIA property implies that  $\gamma_l = 0$  for all  $l$ . Alternatively, IIA is violated if the demand for the factor from country  $j$  relative to

<sup>40</sup>We are grateful to Joe Shapiro for making these data easily accessible to us. For each exporter and year, we compute the freight cost by dividing reported values of total exports CIF by total exports FOB. For domestic sales, we input a freight cost of zero—this is equivalent to assuming a constant (over time) transport cost of domestic sales in the presence of exporter-importer fixed effects.

<sup>41</sup>For each exporter, we compute per capita GDP by dividing the expenditure-side real GDP at current PPP (in 2005 US\$) by the total population. We then construct  $\kappa_j$  as the average per capita GDP between 1992 and 1995.

TABLE 1—REDUCED-FORM ESTIMATES AND VIOLATION OF IIA IN GRAVITY ESTIMATION

Dependent var.: $\Delta\Delta \log(\text{exports})$	(1)	(2)	(3)	(4)
$\Delta\Delta \log(\text{freight cost})$	-5.955 (0.995)	-6.239 (1.100)	-1.471 (0.408)	-1.369 (0.357)
<i>Test for joint significance of interacted competitors' freight costs (<math>H_0 : \gamma_l = 0</math> for all <math>l</math>)</i>				
<i>F-stat</i>	110.34		768.63	
<i>p-value</i>	< 0.001		< 0.001	
<i>Disaggregation level</i>	exporter		exporter-industry	
<i>Observations</i>	576		8,880	

*Notes:* Sample of exports from 37 countries to Australia and United States between 1995 and 2010 (aggregate and 2-digit industry-level). The notation  $\Delta\Delta$  refers to the double-difference (first with respect to one exporting country, the United States, and second across the two importing countries). All models include a full set of dummy variables for exporter(-industry). Standard errors clustered by exporter are reported in parentheses.

the reference country depends also on the price of the factor from country  $l$  (i.e., if  $\gamma_l \neq 0$  for some exporter  $l$ ). The interaction between  $z_{li,t}^\tau$  and  $|\kappa_j - \kappa_l|$  relates this third country effect to the proximity of competitors in terms of per capita GDP.

Table 1 reports estimates of various versions of equation (33). Column 1 begins by restricting attention to the standard CES case in which  $\gamma_l = 0$  for all  $l$ . We obtain an estimate of  $-5.95$  for the trade elasticity, in line with a vast literature that has estimated such a specification: see, e.g., Head and Mayer (2014). Column 2 then includes the interaction terms to estimate the set of coefficients  $\gamma_l$ . Because there are 37 such coefficients and we are only interested in testing whether at least one of them is nonzero, we simply report the value of the  $F$ -test for the hypothesis that  $\gamma_l = 0$  for all  $l$ . This test is rejected at the 1 percent level, while clustering standard errors at the exporter level. Columns 3 and 4 estimate the same specification using trade data disaggregated by 2-digit industry. This exercise investigates whether the IIA violation is simply related to industry aggregation. Accordingly, we allow the exporter fixed effects to be industry-specific as well which implies that parameters are estimated from within-industry variation. For expositional purposes, we impose the same coefficients  $\bar{\epsilon}$  and  $\gamma_l$  across sectors. The hypothesis that  $\gamma_l = 0$  for all  $l$  is again rejected.

To summarize, Table 1 supports the relevance of third-country effects as captured by the interaction between competitor's freight costs and distance between per capita GDPs,  $|\kappa_j - \kappa_l|(\ln z_{li,t}^\tau - \ln z_{l1,t}^\tau)$ . In the structural estimation below, we rely on exactly this variation to obtain estimates of the parameters controlling the cross-price elasticity,  $\sigma_\alpha$  and  $\sigma_\epsilon$ .

*Structural Estimation.*—We now turn to our estimates of  $\theta$  obtained from the procedure described in Section VB. Using the vector of instruments  $\mathbf{Z}_{ji,t}$ , we construct 74 moment conditions to estimate the three structural parameters of interest,  $\{\bar{\epsilon}, \sigma_\alpha, \sigma_\epsilon\}$ , and the 36 exporter fixed effects,  $\{\zeta_j\}$ .<sup>42</sup> Table 2 reports the estimates

<sup>42</sup>Since we only have two importers in our dataset, the exporter-importer terms,  $\zeta_{ji} \equiv -(\Delta \varphi_{ji} - \Delta \varphi_{j1}) - (\Delta \ln \mu_{ji} - \Delta \ln \mu_{j1})$ , in equation (31) reduce to a vector of exporter dummies. The 74 moment conditions



TABLE 2—GMM ESTIMATES OF MIXED CES DEMAND

	$\bar{\epsilon}$	$\sigma_\alpha$	$\sigma_\epsilon$
<i>Panel A. CES</i>	-5.955 (0.950)		
<i>Panel B. Mixed CES (restricted heterogeneity)</i>	-6.115 (0.918)	2.075 (0.817)	
<i>Panel C. Mixed CES (unrestricted heterogeneity)</i>	-6.116 (0.948)	2.063 (0.916)	0.003 (0.248)

Notes: Sample of exports from 37 countries to Australia and United States between 1995 and 2010. All models include 36 exporter dummies. One-step GMM estimator described in Appendix B. Standard errors clustered by exporter are reported in parentheses.

obtained with the one-step GMM estimator using the optimal weights under homoskedasticity, along with their accompanying standard errors clustered by exporter.

In panel A, we restrict  $\sigma_\alpha = \sigma_\epsilon = 0$  in which case we estimate  $\bar{\epsilon}$  to be approximately  $-6$ . As expected, this value is identical to the estimate in column 1 of Table 1.<sup>43</sup> Panel B reports our estimates with unobserved heterogeneity only in  $\alpha$ , whereas panel C focuses on our preferred specification with unobserved heterogeneity in both  $\alpha$  and  $\epsilon$ . As can be seen from panel C, we estimate a value of  $\sigma_\epsilon$  close to zero, indicating that deviations from IIA based on market shares are not important. However, the estimate of  $\sigma_\alpha$  is statistically significant which suggests that we can confidently reject the model in which IIA deviations are unrelated to per capita GDP.<sup>44</sup>

To get more intuition about the economic implications of our structural estimates, Figure 1 plots the cross price-elasticity in equation (30), of demand for an exporter’s factor relative to that of the United States, with respect to a change in Chinese trade costs. This is shown for all exporters except for China in order to focus on cross-price effects. While this elasticity is identically equal to zero (due to the IIA property) in the CES system of panel A, this need not be the case for the other specifications. Indeed, the parameters estimated in panel C imply that the elasticity of relative demand to the relative price of the Chinese factor is positive (statistically different from zero for virtually all countries) and decreasing in per capita GDP.

correspond to those obtained from: the own-cost instrument,  $\Delta \ln(z^T)_{j,i,t} - \Delta \ln(z^T)_{j1,t}$ ; the 37 competitors’ instruments,  $|\kappa_j - \kappa_l|(\ln z^T_{l,i,t} - \ln z^T_{l1,t})$ , one for each exporter in our dataset; and the 36 exporter dummies, one for each exporter in our dataset, except the United States, our reference country.

<sup>43</sup>The standard error in column 1 of Table 1 is slightly larger than that in panel A of Table 2. This difference follows from the degrees of freedom adjustment used in Table 1 that, as noted by Angrist and Pischke (2008), improves the small sample properties of the covariance matrix estimator in the context of linear regressions. For the GMM estimator, there is not a standard degree of freedom adjustment and, therefore, we report the estimate of the asymptotic covariance matrix as described in Appendix B.

<sup>44</sup>In our preferred model of panel C, there are 35 overidentification restrictions. A *J*-test indicates that we cannot reject the null hypothesis that all moment conditions are satisfied.



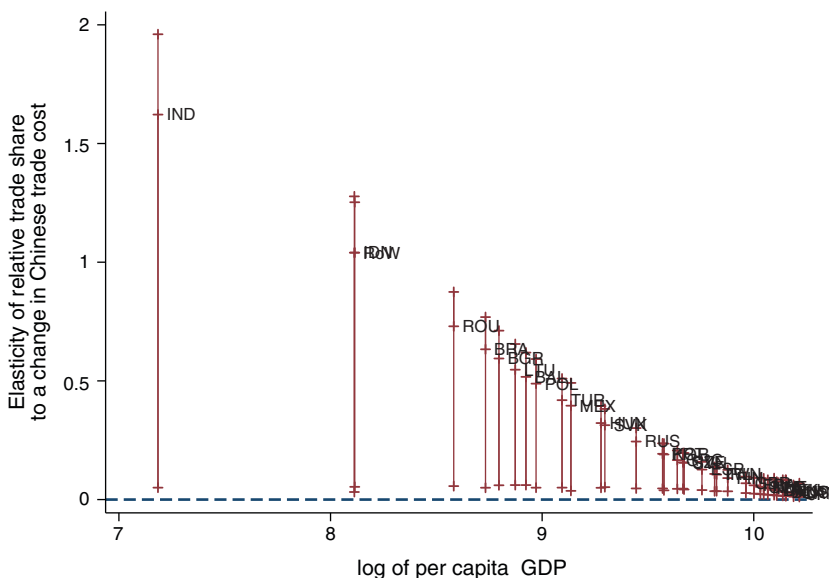


FIGURE 1. ELASTICITY OF DEMAND RELATIVE TO THE UNITED STATES WITH RESPECT TO CHINESE FACTOR PRICE

*Notes:* Elasticity of US demand for factors from any country relative to US demand for US factors with respect to a change in the Chinese factor price. Elasticities are computed using the estimates of the mixed CES demand system in panel C of Table 2. Ninety-five percent confidence intervals shown are computed using the bootstrap procedure described in Appendix D. Dashed line corresponds to the CES case.

## VI. Application: China's Integration in the World Economy

We conclude by applying our methodology to study the consequences of one particular counterfactual: China's integration into the world economy. The goal is to illustrate the potential importance of flexible functional forms through a specific, but important example. Earlier discussions of the China shock can be found in Hanson and Robertson (2010); Fieler (2011); Hsieh and Ossa (2016); and Autor, Dorn, and Hanson (2013), among many others.

We proceed in two steps. First, we use the demand system estimated in Section V to infer the trade costs faced by China, both as an exporter and an importer, at different points in time. Given estimates of Chinese trade costs, we then ask: "For any country  $j$ , how much higher (or lower) would welfare have been at a given year  $t \geq 1995$  if Chinese trade costs were those of 1995 rather than those of year  $t$ ?" The next subsection focuses on the estimation of trade costs. Counterfactual predictions will be discussed in Section VI B.<sup>45</sup>

<sup>45</sup> We follow a two-step procedure because we are interested in quantifying the welfare consequences of China's observed integration—interpreted as changes in iceberg trade costs within our theoretical framework—over the last two decades. Of course, one could dispense with the first step and directly study the effects of arbitrarily chosen changes in trade costs, including those not featuring the normalizations imposed in Section VI A. This is the approach followed in most recent quantitative papers: see, e.g., Costinot and Rodríguez-Clare (2014).

### A. Trade Costs

We measure trade costs as follows. For each importer  $i$  and each year  $t$  in our sample, we start by inverting our demand system,  $\chi_i$ , to go from the vector of expenditure shares,  $\mathbf{x}_{i,t}$ , to the vector of relative effective factor prices,  $\{\omega_{ji,t}/\omega_{1i,t}\}$ . We then use the time series of relative effective factor prices,  $\omega_{ji,t}/\omega_{1i,t} = \chi_{ji}^{-1}(\mathbf{x}_{i,t})$ , and the identity,  $\omega_{ji,t} \equiv \tau_{ji,t}c_{j,t}$ , to construct the time series of iceberg trade costs,  $\{\tau_{ji,t}\}$ , such that

$$(34) \quad (\tau_{ji,t}/\tau_{ii,t})/(\tau_{jj,t}/\tau_{ij,t}) = (\chi_{ji}^{-1}(\mathbf{x}_{i,t})/\chi_{ii}^{-1}(\mathbf{x}_{i,t})) / (\chi_{jj}^{-1}(\mathbf{x}_{j,t})/\chi_{ij}^{-1}(\mathbf{x}_{j,t})),$$

for all  $i, j$ , and  $t$ .

This (log) difference-in-differences provides a nonparametric generalization of the Head and Ries’s (2001) index used to measure trade costs in gravity models. Compared to the case of a CES demand system, the only distinction is that one cannot directly read the difference-in-differences in effective prices from the difference-in-differences in expenditure shares. Inverting demand now requires a computer.

In order to go from a difference-in-differences to the level of Chinese trade costs, we follow the same approach as Head and Ries (2001) and further assume that

$$(35) \quad \tau_{ii,t}/\tau_{ii,95} = 1 \quad \text{for all } i \text{ and } t,$$

$$(36) \quad \tau_{ij,t}/\tau_{ij,95} = \tau_{ji,t}/\tau_{ji,95} \quad \text{for all } t \text{ if } i \text{ or } j \text{ is China.}$$

The first condition rules out differential changes in domestic trade costs around the world, whereas the second condition rules out asymmetric changes in Chinese trade costs.<sup>46</sup> Given equations (34)–(36), we can then measure the proportional changes in Chinese trade costs between 1995 and any period  $t$  as

$$\tau_{ji,t}/\tau_{ji,95} = \sqrt{\frac{(\chi_{ji}^{-1}(\mathbf{x}_{i,t})/\chi_{ii}^{-1}(\mathbf{x}_{i,t})) / (\chi_{jj}^{-1}(\mathbf{x}_{j,t})/\chi_{ij}^{-1}(\mathbf{x}_{j,t}))}{(\chi_{ji}^{-1}(\mathbf{x}_{i,95})/\chi_{ii}^{-1}(\mathbf{x}_{i,95})) / (\chi_{jj}^{-1}(\mathbf{x}_{j,95})/\chi_{ij}^{-1}(\mathbf{x}_{j,95}))}}, \text{ if } i \text{ or } j \text{ is China.}$$

By construction, changes in exporting and importing costs from China are the same, though they may vary across trading partners and over time.

Figure 2 reports the arithmetic average of changes in Chinese trade costs across all trading partners. The solid line corresponds to our baseline estimates, obtained under mixed CES (panel C of Table 2). As can be seen, these are substantial

<sup>46</sup>Our focus on symmetric changes in Chinese trade costs is partly motivated by the desire stay as close as possible to existing practices in the gravity literature. It should be clear, however, that while some normalization is required to go from difference-in-differences to the levels of trade costs, equations (35) and (36) provide only one of many possibilities. For example, an alternative would be to allow bilaterally asymmetric changes in Chinese trade costs under the assumption that some reference country’s trade costs are constant over time. This is akin to focusing on counterfactuals in which one asks what would have happened if China had integrated with the rest of the world to the same extent as that reference country.

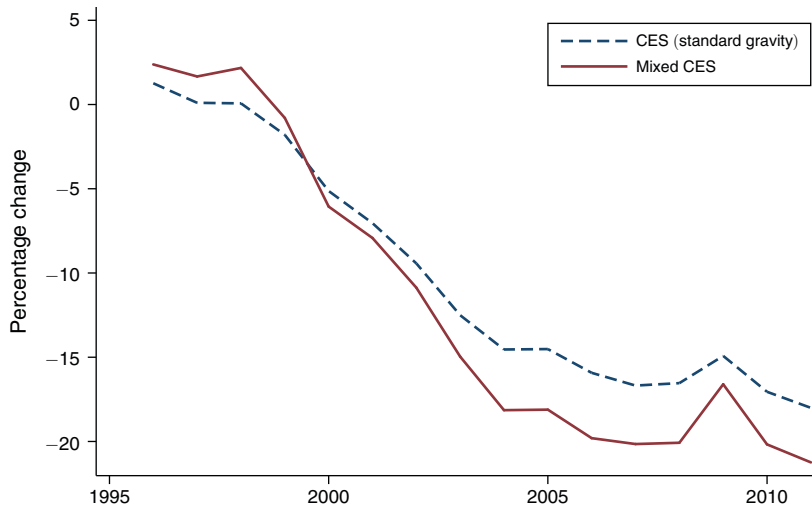


FIGURE 2. AVERAGE TRADE COST CHANGES SINCE 1995: CHINA, 1996–2011

Notes: Arithmetic average across all trading partners in the percentage reduction in Chinese trade costs between 1995 and each year  $t = 1996, \dots, 2011$ . CES (standard gravity) and mixed CES plot the estimates of trade costs obtained using the factor demand system in panels A and C, respectively, of Table 2.

changes in trade costs. Between 1995 and 2007, we estimate that Chinese trade costs decreased by 20.2 percent on average. If we were to restrict ourselves to a CES demand system (the dashed line), the decrease in Chinese trade costs would be equal to 16.7 percent instead.

### B. Counterfactual Predictions

In any year  $t$ , we are interested in counterfactual changes in trade costs,  $\hat{\tau}_{ji,t}$ , such that Chinese trade costs are brought back to their 1995 levels:

$$(37) \quad \hat{\tau}_{ji,t} = \tau_{ji,95} / \tau_{ji,t}, \quad \text{if } i \text{ or } j \text{ is China,}$$

$$(38) \quad \hat{\tau}_{ji,t} = 1, \quad \text{otherwise.}$$

Given estimates of the factor demand system, obtained in Section V, and estimates of trade costs, obtained in Section VIA, we can use Corollary 1 to compute the welfare changes associated with this counterfactual scenario.<sup>47</sup>

Figure 3 reports the negative of the welfare changes in China for all years in our sample. A positive number in year  $t$  corresponds to the gains from economic integration for China between 1995 and year  $t$ . Before the great trade collapse in 2007, we see that the gains from economic integration for China are equal to 1.54 percent. In

<sup>47</sup>Our counterfactual calculations allow for lump-sum transfers between countries to rationalize trade imbalances in the initial equilibrium. We then hold these lump-sum transfers constant across the initial and counterfactual equilibria. Details on the algorithm for the computation of the counterfactual exercise are described in Appendix D.

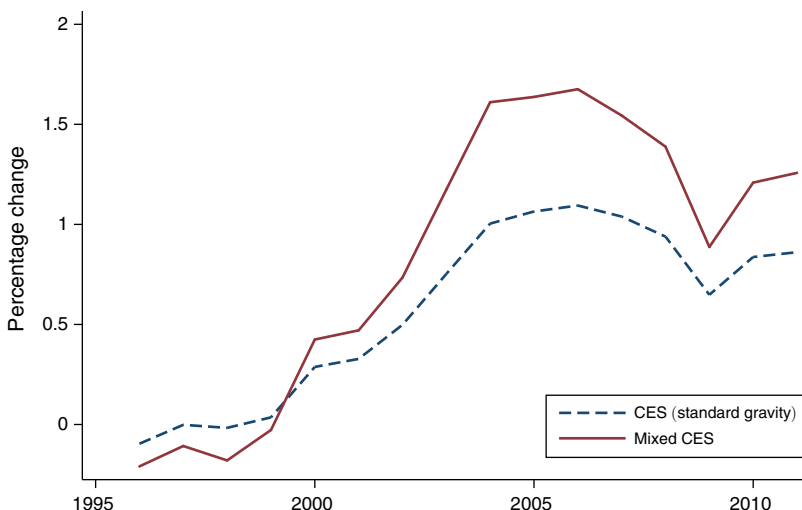


FIGURE 3. WELFARE GAINS FROM CHINESE INTEGRATION SINCE 1995: CHINA, 1996–2011

Notes: Welfare gains in China from reduction in Chinese trade costs relative to 1995 in each year  $t = 1996, \dots, 2011$ . CES (standard gravity) and mixed CES plot the estimates of welfare changes obtained using the factor demand system in panels A and C, respectively, of Table 2.

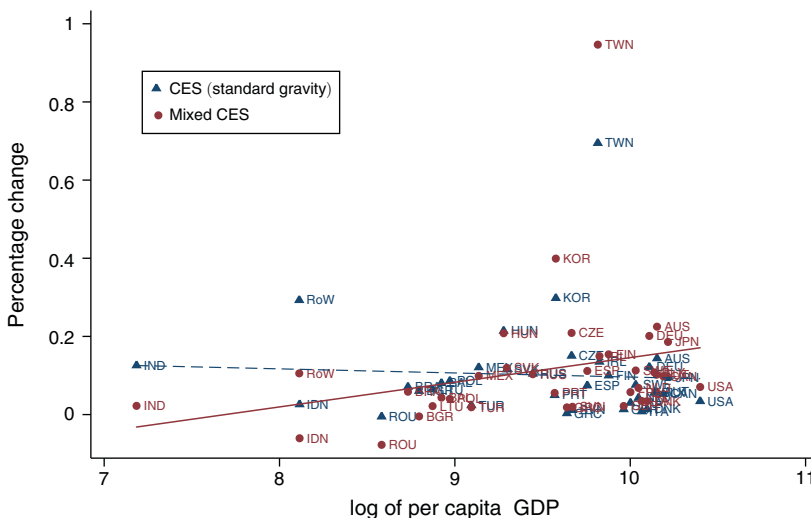


FIGURE 4. WELFARE GAINS FROM CHINESE INTEGRATION SINCE 1995: OTHER COUNTRIES, 2007

Notes: Welfare gains in other countries from reduction in Chinese trade costs relative to 1995 in year  $t = 2007$ . CES (standard gravity) and mixed CES plot the estimates of welfare changes obtained using the factor demand system in panels A and C, respectively, of Table 2. The solid line shows the line of best fit through the mixed CES points, and the dashed line the equivalent for the CES case. Bootstrapped 95 percent confidence intervals for these estimates are reported in Table A2.

line with our estimates of trade costs, we see that imposing CES would instead lead to gains from economic integration equal to 1.04 percent.

What about China’s trading partners? Figure 4 reports the welfare change from bringing Chinese trade costs back to their 1995 levels for all other countries in 2007.

The bootstrapped 95 percent confidence intervals corresponding to each of these estimates (as well as those for China) can be found in Table A2 in Appendix D. Under our preferred estimates (circles), we see that rich countries tend to gain relatively more from China's integration, with Romania experiencing a statistically significant loss. The previous pattern gets muted if one forces factor demand to be CES instead (triangles).<sup>48</sup>

## VII. Concluding Remarks

This paper starts from a simple observation. If neoclassical trade models are like exchange economies in which countries trade factor services, then the shape of these countries' reduced factor demand must be sufficient for answering many counterfactual questions.

Motivated by this observation, we have developed tools to conduct counterfactual and welfare analysis given knowledge of any factor demand system. Then, we have provided sufficient conditions under which estimates of this system can be recovered nonparametrically. Lastly, we have applied our tools to study a particular counterfactual question: what would have happened to other countries if China had remained closed? Since the answer to this question hinges on how substitutable factors of production from around the world are, we have introduced a parsimonious generalization of the CES demand system that allows for rich patterns of substitution across factors from different countries. The counterfactual results based on estimates of this system illustrate the feasibility and potential benefits of allowing trade data to speak with added flexibility.

Clearly, our emphasis on reduced factor demand also has costs. The demand system in our empirical application remains high-dimensional. We consider a world economy with 37 exporters, but data are limited—freight costs for these 37 exporters are only available for 16 years and 2 importers. So parametric restrictions need to be imposed. The typical approach is to impose such restrictions on deeper primitives of the model, like preferences and technology, and then to use various data sources to estimate or calibrate each of those fundamentals.<sup>49</sup> Here, we propose instead to impose restrictions directly on the factor demand system, while building estimation on precisely the moment conditions under which we have shown this system to be nonparametrically identified. Given data constraints, we do not view our approach as a panacea. But we believe that the tight connection between theory and data that it offers makes it worthy of further investigation.

An important open question concerns the extent to which one could combine the approach in this paper with additional, more disaggregated data sources. The answer is likely to depend on the additional assumptions that one is willing to impose, with costs and benefits that will need to be weighed. Consider, for instance, the differences in patterns of specialization across sectors and countries. Intuitively, there is a lot of information to be gained from such sector-level data. But if one is interested

<sup>48</sup> Away from the CES case, Fieler (2011) also documents heterogeneous effects of China's growth across countries. In an economy with nonhomothetic preferences, she finds that China's rich and poor neighbors tend to benefit the most, whereas China's middle-income neighbors lose.

<sup>49</sup> Bas, Mayer, and Thoenig (2015) provides an interesting example of this approach in the context of monopolistically competitive models of international trade.

in aggregate questions, such data never come for free; disaggregated data will need to be aggregated ultimately. One possibility would be to use sector-level data, say in the presample period, to construct additional observed country characteristics in a factor demand system akin to the one introduced in Section V. Another possibility, closer to existing work, would be to maintain strong functional forms on the way that sector-level factor demands are aggregated, but allow for mixed CES demand systems to deal flexibly with the substantial unobserved heterogeneity across goods within narrowly defined sectors: see Schott (2004).

Regardless of the methodology that one chooses, we hope that our theoretical results can make more transparent how CGE models map data into counterfactual predictions. One cannot escape Manski's (2003, p. 1) Law of Decreasing Credibility, that "the credibility of inference decreases with the strength of the assumptions maintained." But identifying the critical assumptions upon which counterfactual predictions rely in complex general equilibrium environments can help evaluate their credibility. Once it is established that assumptions about the shape of factor demand—and only the shape of factor demand—determine counterfactual predictions, it becomes easier to ask whether the moments chosen for structural estimation are related to the economic relation of interest and to explore whether functional form assumptions rather than data drive particular results.

In terms of applications, two lines of research seem particularly promising. The first concerns the distributional consequences of international trade. By assuming the same factor intensity in all sectors, our empirical application assumes away distributional issues. None of the theoretical results in Sections II and III, however, rely on this assumption. Hence, the same nonparametric approach could be used to study the impact of globalization on the skill premium or the relative return to capital. The second line of research concerns the consequences of factor mobility, either migration or foreign direct investment. Although factor supply is inelastic in Section II, it would be easy to incorporate such considerations by introducing intermediate goods, as we did in Section III C. Then either migration or foreign direct investment would be equivalent to trade in intermediate goods, which may be subject to different frictions than trade in final goods.

Finally, while we have emphasized counterfactual and welfare analysis in this paper, the tools that we have developed could be applied more generally. Many questions concerning international trade can be reduced to estimating and inverting a demand system. But this system does not have to be CES. In Section VI A, we have already mentioned the measurement of trade costs, which is an important application of gravity models: see, e.g., Anderson and van Wincoop (2004) and Jacks, Meissner, and Novy (2011). Another natural application is the measurement of comparative advantage: see, e.g., Costinot, Donaldson, and Komunjer (2012) and Levchenko and Zhang (2016). Measures of revealed comparative advantage (RCA) aim to uncover which countries can produce and sell goods relatively more cheaply, and this boils down to a difference-in-differences of  $(\log)$ prices. Away from CES, this difference-in-differences will not be proportional to a difference-in-differences of  $(\log)$ expenditures. But given estimates of any invertible demand system, RCA remains an easy object to compute.

## APPENDIX A: PROOFS

## A. Proposition 1

PROOF OF PROPOSITION 1:

( $\Rightarrow$ ) Suppose that  $(\mathbf{q}, \mathbf{l}, \mathbf{p}, \mathbf{w})$  is a competitive equilibrium. For any country  $i$ , let us construct  $\mathbf{L}_i \equiv \{L_{ji}^n\}$  such that

$$L_{ji}^n = \sum_k l_{ji}^{nk} \quad \text{for all } i, j, \text{ and } n.$$

Together with the factors market clearing condition (5), the previous expression immediately implies

$$\sum_j L_{ij}^n = v_i^n \quad \text{for all } i \text{ and } n.$$

In order to show that  $(\mathbf{L}, \mathbf{w})$  is a reduced equilibrium, we therefore only need to show

$$(39) \quad \mathbf{L}_i \in \arg \max_{\tilde{\mathbf{L}}_i} U_i(\tilde{\mathbf{L}}_i),$$

$$\sum_{j,n} w_j^n \tilde{L}_{ji}^n \leq \sum_n w_i^n v_i^n \quad \text{for all } i.$$

We proceed by contradiction. Suppose that there exists a country  $i$  such that condition (39) does not hold. Since profits are zero in a competitive equilibrium with constant returns to scale, we must have  $\sum_{j,k} p_{ji}^k q_{ji}^k = \sum_{j,n} w_j^n L_{ji}^n$ . The budget constraint of the representative agent in the competitive equilibrium, in turn, implies  $\sum_{j,n} w_j^n L_{ji}^n = \sum_n w_i^n v_i^n$ . Accordingly, if condition (39) does not hold, there must be  $\mathbf{L}'_i$  such that  $U_i(\mathbf{L}'_i) > U_i(\mathbf{L}_i)$  and  $\sum_{j,n} w_j^n (L'_{ji})' \leq \sum_n w_i^n v_i^n$ . Now consider  $(\mathbf{q}'_i, \mathbf{l}'_i)$  such that

$$(\mathbf{q}'_i, \mathbf{l}'_i) \in \arg \max_{\tilde{\mathbf{q}}_i, \tilde{\mathbf{l}}_i} u_i(\tilde{\mathbf{q}}_i),$$

$$\sum_k \tilde{l}_{ji}^{nk} \leq (L'_{ji})' \quad \text{for all } j \text{ and } n,$$

$$\tilde{q}_{ji}^k \leq f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) \quad \text{for all } j \text{ and } k.$$

We must have

$$u_i(\mathbf{q}'_i) = U_i(\mathbf{L}'_i) > U_i(\mathbf{L}_i) \geq u_i(\mathbf{q}_i),$$

where the last inequality derives from the fact that, by construction,  $\mathbf{L}_i$  is sufficient to produce  $\mathbf{q}_i$ . Utility maximization in the competitive equilibrium therefore implies

$$\sum_{j,k} p_{ji}^k (q_{ji}^k)' > \sum_n w_i^n v_i^n.$$



Combining this inequality with  $\sum_{j,n} w_j^n (L_{ji}^n)' \leq \sum_n w_i^n v_i^n$ , we obtain

$$\sum_{j,k} p_{ji}^k (q_{ji}^k)' > \sum_{j,n} w_j^n (L_{ji}^n)'.$$

Hence, firms could make strictly positive profits by using  $\mathbf{L}'_i$ , to produce  $\mathbf{q}'_i$ , which cannot be true in a competitive equilibrium. This establishes that  $(\mathbf{L}, \mathbf{w})$  is a reduced equilibrium with the same factor prices and the same factor content of trade as the competitive equilibrium. The fact that  $U_i(\mathbf{L}_i) = u_i(\mathbf{q}_i)$  can be established in a similar manner. If there were  $\mathbf{q}'_i$  such that  $u_i(\mathbf{q}'_i) = U_i(\mathbf{L}_i) > u_i(\mathbf{q}_i)$ , then utility maximization would imply

$$\sum_{j,k} p_{ji}^k (q_{ji}^k)' > \sum_n w_i^n v_i^n = \sum_{j,n} w_j^n L_{ji}^n,$$

which would in turn violate profit maximization in the competitive equilibrium.

( $\Leftarrow$ ) Suppose that  $(\mathbf{L}, \mathbf{w})$  is a reduced equilibrium. For any positive vector of output delivered in country  $i$ ,  $\mathbf{q}_i \equiv \{q_{ji}^k\}$ , let  $C_i(\mathbf{w}, \mathbf{q}_i)$  denote the minimum cost of producing  $\mathbf{q}_i$ :

$$(40) \quad C_i(\mathbf{w}, \mathbf{q}_i) \equiv \min_{\tilde{\mathbf{l}}_i} \sum_{j,k,n} w_j^n \tilde{l}_{ji}^{nk}$$

$$(41) \quad q_{ji}^k \leq f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) \quad \text{for all } j \text{ and } k.$$

The first step of our proof characterizes basic properties of  $C_i$ . The last two steps use these properties to construct a competitive equilibrium that replicates the factor content of trade and the utility levels in the reduced equilibrium.

**Step 1:** For any country  $i$ , there exists  $\mathbf{p}_i \equiv \{p_{ji}^k\}$  positive such that the two following conditions hold: (i)

$$(42) \quad C_i(\mathbf{w}, \mathbf{q}_i) = \sum_{j,k} p_{ji}^k q_{ji}^k, \quad \text{for all } \mathbf{q}_i > 0,$$

and (ii) if  $\mathbf{l}_i$  solves (40), then  $\mathbf{l}_i$  solves

$$(43) \quad \max_{\tilde{\mathbf{l}}_{ji}^k} p_{ji}^k f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) - \sum_n w_j^n \tilde{l}_{ji}^{nk} \quad \text{for all } j \text{ and } k.$$

To show this for any  $i, j$ , and  $k$ , let us construct  $p_{ji}^k$  such that

$$(44) \quad p_{ji}^k = \min_{\tilde{\mathbf{l}}_{ji}^k} \left\{ \sum_n w_j^n \tilde{l}_{ji}^{nk} \mid f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) \geq 1 \right\}.$$

Take  $\mathbf{l}_{ji}^k(1)$  that solves the previous unit cost minimization problem. Since  $f_{ji}^k$  is homogeneous of degree 1, we must have  $f_{ji}^k(q_{ji}^k \mathbf{l}_{ji}^k(1)) \geq q_{ji}^k$ . By definition of  $C_i$ , we must also have  $C_i(\mathbf{w}, \mathbf{q}_i) \leq \sum_{j,k,n} q_{ji}^k w_j^n \tilde{l}_{ji}^{nk}(1) = \sum_{j,k} p_{ji}^k q_{ji}^k$ . To show that

equation (42) holds, we therefore only need to show that  $C_i(\mathbf{w}, \mathbf{q}_i) \geq \sum_{j,k} p_{ji}^k q_{ji}^k$ . We proceed by contradiction. Suppose that  $C_i(\mathbf{w}, \mathbf{q}_i) < \sum_{j,k} p_{ji}^k q_{ji}^k$ . Then there must be  $q_{ji}^k > 0$  such that

$$\sum_n w_j^n l_{ji}^{nk} < q_{ji}^k \sum_n w_j^n l_{ji}^{nk}(1),$$

where  $\mathbf{l}_{ji}^k$  is part of the solution of (40). Since  $f_{ji}^k$  is homogeneous of degree 1,  $\mathbf{l}_{ji}^k/q_{ji}^k$  would then lead to strictly lower unit cost than  $\mathbf{l}_{ji}^k(1)$ , which cannot be. This establishes condition (i).

To establish condition (ii), we proceed again by contradiction. Suppose that there exists  $(\tilde{\mathbf{l}}_{ji}^k)'$  such that

$$(45) \quad p_{ji}^k f_{ji}^k((\tilde{\mathbf{l}}_{ji}^k)') - \sum_n w_j^n (l_{ji}^{nk})' > p_{ji}^k f_{ji}^k(\mathbf{l}_{ji}^k) - \sum_n w_j^n l_{ji}^{nk}.$$

Take the vector of output  $\mathbf{q}_i$  such that  $q_{ji}^k = f_{ji}^k(\mathbf{l}_{ji}^k)$  and zero otherwise. Condition (i) applied to that vector immediately implies

$$p_{ji}^k f_{ji}^k(\mathbf{l}_{ji}^k) = \sum_n w_j^n l_{ji}^{nk}.$$

Combining this observation with inequality (45), we get  $p_{ji}^k > \sum_n w_j^n (l_{ji}^{nk})' / f_{ji}^k((\tilde{\mathbf{l}}_{ji}^k)')$ , which contradicts the fact that  $p_{ji}^k$  is the minimum unit cost.

**Step 2:** Suppose that  $(\mathbf{q}_i, \mathbf{l}_i)$  solves

$$(46) \quad \max_{\tilde{\mathbf{q}}_i, \tilde{\mathbf{l}}_i} u_i(\tilde{\mathbf{q}}_i),$$

$$\tilde{q}_{ji}^k \leq f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) \quad \text{for all } j \text{ and } k,$$

$$\sum_{j,k,n} w_j^n \tilde{l}_{ji}^{nk} \leq \sum_n w_i^n v_i^n.$$

Then  $\mathbf{q}_i$  solves

$$(47) \quad \max_{\tilde{\mathbf{q}}_i} u_i(\tilde{\mathbf{q}}_i),$$

$$\sum_{j,k} p_{ji}^k \tilde{q}_{ji}^k \leq \sum_n w_i^n v_i^n,$$

and  $\mathbf{l}_i$  solves

$$(48) \quad \max_{\tilde{\mathbf{l}}_{ji}^k} p_{ji}^k f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) - \sum_n w_j^n \tilde{l}_{ji}^{nk} \quad \text{for all } j \text{ and } k.$$

To see this, note that if  $(\mathbf{q}_i, \mathbf{l}_i)$  solves (46), then

$$\mathbf{q}_i \in \arg \max_{\tilde{\mathbf{q}}_i} u_i(\tilde{\mathbf{q}}_i),$$

$$C_i(\mathbf{w}, \tilde{\mathbf{q}}_i) \leq \sum_n w_i^n v_i^n.$$

Combining this observation with Step 1 condition (i), we obtain that  $\mathbf{q}_i$  solves (47). Likewise, if  $(\mathbf{q}_i, \mathbf{l}_i)$  solves (46), then

$$\mathbf{l}_i \in \arg \min_{\tilde{\mathbf{l}}_i} \sum_{j,k,n} w_j^n \tilde{l}_{ji}^{nk},$$

$$q_{ji}^k \leq f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) \quad \text{for all } j \text{ and } k.$$

Combining this observation with Step 1 condition (ii), we obtain that  $\mathbf{l}_i$  solves (48).

**Step 3:** For all  $i$ , take  $(\mathbf{q}_i, \mathbf{l}_i)$  that solves

$$(49) \quad \max_{\tilde{\mathbf{q}}_i, \tilde{\mathbf{l}}_i} u_i(\tilde{\mathbf{q}}_i),$$

$$\tilde{q}_{ji}^k \leq f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k) \quad \text{for all } j \text{ and } k,$$

$$\sum_k \tilde{l}_{ji}^{nk} \leq L_{ji}^n \quad \text{for all } j \text{ and } n,$$

and set  $\{\mathbf{q}\} = \{\mathbf{q}_i\}$  and  $\{\mathbf{l}\} = \{\mathbf{l}_i\}$ . Then  $(\mathbf{q}, \mathbf{l}, \mathbf{p}, \mathbf{w})$  is a competitive equilibrium with (i) the same factor prices,  $\mathbf{w}$ ; (ii) the same factor content of trade,  $L_{ji}^n = \sum_k l_{ji}^{nk}$  for all  $i, j$ , and  $n$ ; and (iii) the same welfare levels,  $U_i(\mathbf{L}_i) = u_i(\mathbf{q}_i)$  for all  $i$ .

To see this, note that since  $(\mathbf{L}, \mathbf{w})$  is a reduced equilibrium, if  $(\mathbf{q}_i, \mathbf{l}_i)$  solves (49), then  $(\mathbf{q}_i, \mathbf{l}_i)$  solves (46). By Step 2,  $\mathbf{q}_i$  and  $\mathbf{l}_i$  must therefore solve (47) and (48), respectively. Hence, the utility maximization and profit maximization conditions (1) and (3) are satisfied. Since the constraint  $\tilde{q}_{ji}^k \leq f_{ji}^k(\tilde{\mathbf{l}}_{ji}^k)$  must be binding for all  $j$  and  $k$  in any country  $i$ , the good market clearing condition (4) is satisfied as well. The factor market clearing condition directly derives from the fact that  $(\mathbf{L}, \mathbf{w})$  is a reduced equilibrium and the constraint,  $\sum_k \tilde{l}_{ji}^{nk} \leq L_{ji}^n$ , must be binding for all  $j$  and  $n$  in any country  $i$ . By construction, conditions (i)–(iii) necessarily hold. ■

### B. Lemma 1

#### PROOF OF LEMMA 1:

We proceed in two steps.

**Step 1:** In a Ricardian economy, if good expenditure shares satisfy the connected substitutes property, then factor expenditure shares satisfy the connected substitutes property.

Our goal is to establish that factor demand,  $\chi_i$ , satisfies the connected substitutes property—expressed in terms of the effective prices of the composite factors,  $\omega_i \equiv \{\tau_{ji}c_j\}$ —if good demand,  $\sigma_i$ , satisfies the connected substitutes property, with

$$\sigma_i(\mathbf{p}_i) \equiv \left\{ \{s_i^k\} \mid s_i^k = p_i^k q_i^k / y_i \text{ for some } \mathbf{q}_i \in \arg \max_{\tilde{\mathbf{q}}_i} \left\{ \bar{u}_i(\tilde{\mathbf{q}}_i) \mid \sum_k p_i^k \tilde{q}_i^k \leq y_i \right\} \right\}.$$

Note that since  $\bar{u}_i$  is homothetic,  $\sigma_i$  does not depend on income in country  $i$ .

Consider a change in effective factor prices from  $\omega_i$  to  $\omega'_i$  and a partition of countries  $\{M_1, M_2\}$  such that  $\omega'_{ji} > \omega_{ji}$  for all  $j \in M_1$  and  $\omega'_{ji} = \omega_{ji}$  for all  $j \in M_2$ . Now take  $\mathbf{x}_i, \mathbf{x}'_i > 0$  such that  $\mathbf{x}_i \in \chi_i(\omega_i)$  and  $\mathbf{x}'_i \in \chi_i(\omega'_i)$ . For each exporting country  $j$ , we can decompose total expenditure shares into the sum of expenditure shares across all sectors  $k$ ,

$$x_{ji} = \sum_k s_i^k x_{ji}^k,$$

where  $s_i^k$  denotes the share of expenditure on good  $k$  in country  $i$  at the initial prices,

$$\begin{aligned} \{s_i^k\} &\in \sigma_i(\{p_i^k(\omega_i)\}), \\ p_i^k(\omega_i) &= \min_j \{\omega_{ji} / \alpha_{ji}^k\}. \end{aligned}$$

For any good  $k$ , there are two possible cases. If no country  $j \in M_2$  has the minimum cost for good  $k$  at the initial factor prices,  $\omega_i$ , then

$$(50) \quad \sum_{j \in M_2} x_{ji}^k = 0,$$

$$(51) \quad p_i^k(\omega_i) < p_i^k(\omega'_i).$$

Let us call this set of goods  $K_1$ . If at least one country  $i \in M_2$  has the minimum cost for good  $k$ , then

$$(52) \quad \sum_{j \in M_2} (x_{ji}^k)' = 1,$$

$$(53) \quad p_i^k(\omega_i) = p_i^k(\omega'_i).$$

Let us call this second set of goods  $K_2$ . Since  $\mathbf{x}_i, \mathbf{x}'_i > 0$ , we know that both  $K_1$  and  $K_2$  are nonempty.

Now consider the total expenditure in country  $i$  on factors from countries  $j \in M_2$  when factor prices are equal to  $\omega'_i$ . It must satisfy

$$\sum_{j \in M_2} (x_{ji})' \geq \sum_{j \in M_2} \sum_{k \in K_2} (s_i^k)' (x_{ji}^k)' = \sum_{k \in K_2} (s_i^k)' \left[ \sum_{j \in M_2} (x_{ji}^k)' \right].$$

Combining the previous inequality with (52), we obtain

$$\sum_{j \in M_2} (x_{ji})' \geq \sum_{k \in K_2} (s_i^k)'$$

By the Inada conditions, all goods are consumed. Thus, we can invoke the connected substitutes property for goods in  $K_1$  and  $K_2$ . Conditions (51) and (53) imply

$$\sum_{k \in K_2} (s_i^k)' > \sum_{k \in K_2} s_i^k.$$

Since  $\sum_{j \in M_2} x_{ji}^k \leq 1$ , the two previous inequalities further imply

$$\sum_{j \in M_2} (x_{ji})' > \sum_{k \in K_2} s_i^k \left[ \sum_{j \in M_2} x_{ji}^k \right] = \sum_{j \in M_2} \sum_{k \in K_2} s_i^k x_{ji}^k.$$

Finally, using (50) and the fact that  $\{K_1, K_2\}$  is a partition, we get

$$\sum_{j \in M_2} (x_{ji})' > \sum_{j \in M_2} \sum_{k \in K_1} s_i^k x_{ji}^k + \sum_{j \in M_2} \sum_{k \in K_2} s_i^k x_{ji}^k = \sum_{j \in M_2} x_{ji}.$$

This establishes that  $\chi_i$  satisfies the connected substitutes property.

**Step 2:** *If factor demand  $\chi_i$  satisfies the connected substitutes property, then for any vector of factor expenditure shares,  $\mathbf{x} > 0$ , there is at most one vector (up to a normalization) of effective factor prices,  $\omega$ , such that  $\mathbf{x} \in \chi_i(\omega)$ .*

We proceed by contradiction. Suppose that there exist  $\omega, \omega'$ , and  $\mathbf{x}_0 > 0$  such that  $\mathbf{x}_0 \in \chi_i(\omega), \mathbf{x}_0 \in \chi_i(\omega')$ , and  $\omega$  and  $\omega'$  are not collinear. Since  $\chi_i$  is homogeneous of degree zero in all factor prices, we can assume without loss of generality that  $\omega_j \geq \omega'_j$  for all  $j$ , with at least one strict inequality and one equality. Now let us partition all countries into two groups,  $M_1$  and  $M_2$ , such that

$$(54) \quad \omega'_j > \omega_j \quad \text{if } j \in M_1,$$

$$(55) \quad \omega'_j = \omega_j \quad \text{if } j \in M_2.$$

Since  $\chi_i$  satisfies the connected substitutes property, conditions (54) and (55) imply that for any  $\mathbf{x}, \mathbf{x}' > 0$  such that  $\mathbf{x} \in \chi_i(\omega)$  and  $\mathbf{x}' \in \chi_i(\omega')$ , we must have

$$\sum_{j \in M_2} x'_j > \sum_{j \in M_2} x_j,$$

which contradicts the existence of  $\mathbf{x}_0 \in \chi_i(\omega) \cap \chi_i(\omega')$ . Lemma 1 follows from Steps 1 and 2. ■

## C. Lemma 2

## PROOF OF LEMMA 2:

We proceed by contradiction. Suppose that there exist two equilibrium vectors of factor prices,  $\mathbf{c} \equiv (c_1, \dots, c_j)$  and  $\mathbf{c}' \equiv (c'_1, \dots, c'_j)$ , that are not collinear. By Proposition 1, we know that  $\mathbf{c}$  and  $\mathbf{c}'$  must be equilibrium vectors of the reduced exchange model. So they must satisfy

$$(56) \quad \sum_i L_{ji} = \bar{f}_j(\mathbf{v}_j), \quad \text{for all } j,$$

$$(57) \quad \sum_i L'_{ji} = \bar{f}_j(\mathbf{v}_j), \quad \text{for all } j,$$

where  $\{L_{ji}\}$  and  $\{L'_{ji}\}$  are the optimal factor demands in the two equilibria,

$$\{L_{ji}\} \in \mathbf{L}_i(\boldsymbol{\omega}_i), \quad \text{for all } i,$$

$$\{L'_{ji}\} \in \mathbf{L}_i(\boldsymbol{\omega}'_i), \quad \text{for all } i,$$

with  $\boldsymbol{\omega}_i \equiv \{\tau_{ji} c_j\}$  and  $\boldsymbol{\omega}'_i \equiv \{\tau_{ji} c'_j\}$  the associated vectors of effective factor prices.

We can follow the same strategy as in Step 2 of the proof of Lemma 1. Without loss of generality, let us assume that  $c'_j \geq c_j$  for all  $j$ , with at least one strict inequality and one equality. We can again partition all countries into two groups,  $M_1$  and  $M_2$ , such that

$$(58) \quad c'_j > c_j \quad \text{if } j \in M_1,$$

$$(59) \quad c'_j = c_j \quad \text{if } j \in M_2.$$

The same argument then implies that in any country  $i$ ,

$$\sum_{j \in M_2} x'_{ji} > \sum_{j \in M_2} x_{ji},$$

where  $\{x_{ji}\}$  and  $\{x'_{ji}\}$  are the expenditure shares associated with  $\{L_{ji}\}$  and  $\{L'_{ji}\}$ , respectively. By definition of the factor expenditure shares, the previous inequality can be rearranged as

$$\sum_{j \in M_2} c'_j L'_{ji} / (c'_i \bar{f}_i(\mathbf{v}_i)) > \sum_{j \in M_2} c_j L_{ji} / (c_i \bar{f}_i(\mathbf{v}_i)).$$

Since  $c'_i \geq c_i$  for all  $i$ , this implies

$$\sum_{j \in M_2} c'_j L'_{ji} > \sum_{j \in M_2} c_j L_{ji}.$$

Summing across all importers  $i$ , we therefore have

$$\sum_{j \in M_2} c'_j \sum_i L'_{ji} > \sum_{j \in M_2} c_j \sum_i L_{ji}.$$

By equations (56) and (57), this further implies

$$\sum_{j \in M_2} c'_j \bar{f}_j(\boldsymbol{\nu}_j) > \sum_{j \in M_2} c_j \bar{f}_j(\boldsymbol{\nu}_j),$$

which contradicts (59). ■

### APPENDIX B: ESTIMATION

In this section we discuss further details of the estimation procedure outlined in Section VB.

#### A. GMM Estimator

Define the stacked matrix of instruments,  $\mathbf{Z}$ , and the stacked vector of errors,  $\mathbf{e}(\boldsymbol{\theta})$ . The GMM estimator is

$$\hat{\boldsymbol{\theta}} = \arg \min_{\boldsymbol{\theta}} \mathbf{e}(\boldsymbol{\theta})' \mathbf{Z} \Phi \mathbf{Z}' \mathbf{e}(\boldsymbol{\theta}),$$

where  $\Phi$  is the GMM weight. We confine attention to the consistent one-step procedure by setting  $\Phi = (\mathbf{Z}' \mathbf{Z})^{-1}$ .

#### B. Standard Errors

In our baseline specification, we allow for the possibility of autocorrelation in the error term. Specifically, we assume that observations are independent across exporter-importer pairs, but do not impose any restriction on the autocorrelation across periods for the same pair. Following Cameron and Miller (2011), we have that

$$\sqrt{M} (\hat{\boldsymbol{\theta}} - \boldsymbol{\theta}) \rightarrow N[0, (B' \Phi B)^{-1} (B' \Phi \Lambda \Phi B) (B' \Phi B)^{-1}],$$

where  $B \equiv E[Z'_{ji,t} \nabla_{\boldsymbol{\theta}} e_{ji,t}(\boldsymbol{\theta})]$  and  $\Lambda \equiv E[(Z'_{ji} e_{ji})(Z'_{ji} e_{ji})']$ , with  $Z_{ji} = [Z_{ji,t}]_{t=1}^T$  and  $e_{ji} \equiv [e_{ji,t}]_{t=1}^T$  being matrices of stacked periods for exporter-importer pair  $(j, i)$  where  $M = NI$ .

The covariance matrix can be consistently estimated using

$$(60) \quad \widehat{\text{Avar}}(\hat{\boldsymbol{\theta}}) \equiv (\hat{B}' \Phi \hat{B})^{-1} (\hat{B}' \Phi \hat{\Lambda} \Phi \hat{B}) (\hat{B}' \Phi \hat{B})^{-1},$$

where  $\hat{B} \equiv (\mathbf{Z}' \nabla_{\boldsymbol{\theta}} \mathbf{e}(\hat{\boldsymbol{\theta}}))$ , and  $\hat{\Lambda} \equiv \Gamma' \Gamma$  such that  $\Gamma \equiv [e_{ji}(\hat{\boldsymbol{\theta}})' Z_{ji}]_{ji}$ .



This analysis ignored the fact that we take draws of  $(\alpha_s, \epsilon_s)$  to compute simulated moment conditions in the algorithm described below. Although this simulation step affects standard errors, the asymptotic distribution of the estimator is the same as the number of simulated draws goes to infinity. Thus, we compute the covariance matrix according to expression (60) which is assumed to be an appropriate approximation for the large number of simulations (discussed below) used in the empirical implementation.

C. Estimation Algorithm

In order to estimate the model, it is convenient to focus on the following log transformation of effective factor prices,  $\delta_{ji,t} \equiv -\bar{\epsilon} \ln(\mu_{ji}\omega_{ji,t}/\mu_{1i}\omega_{1i,t})$ . Define  $\chi(\delta_{i,t} | \theta_2)$  as the demand system in equation (28) expressed in terms of  $\delta_{i,t} \equiv \{\delta_{ji,t}\}$ , so that

$$(61) \quad \chi_j(\delta_{i,t} | \theta_2) = \int \frac{\exp(\alpha \sigma_\alpha \ln \kappa_j + \epsilon^{\sigma_\epsilon} \delta_{ji,t})}{1 + \sum_{l=2}^N \exp(\alpha \sigma_\alpha \ln \kappa_l + \epsilon^{\sigma_\epsilon} \delta_{li,t})} dF(\alpha, \epsilon)$$

with  $\theta_2 \equiv (\sigma_\alpha, \sigma_\epsilon)$ . As described in Section VB, we can write

$$e_{ji,t}(\theta) \equiv \ln \chi_j^{-1}(\mathbf{x}_{i,t} | \theta_2) - \ln \chi_j^{-1}(\mathbf{x}_{1,t} | \theta_2) - \mathbf{Z}_{ji,t}^1 \cdot \theta_1,$$

with  $\theta_1 = (-\bar{\epsilon}, \{\zeta_{ji}\})$  and  $\mathbf{Z}_{ji,t}^1 \equiv (\Delta \ln(z^\tau)_{ji,t} - \Delta \ln(z^\tau)_{j1,t}, \mathbf{d}_{ji,t})$ .

The simulated GMM procedure is implemented with the following steps.

**Step 0:** Draw  $S$  simulated pairs  $(\alpha_s, \ln \epsilon_s) \sim N(0, I)$ . We set  $S = 4,000$  and use the same draws for all markets.

**Step 1:** Conditional on  $\theta_2$ , compute the vector  $\chi^{-1}(\mathbf{x}_{i,t} | \theta_2) \equiv \{\delta_{ji,t}\}_{j=2}^N$  that solves the following system:

$$\{\chi_j(\delta_{i,t} | \theta_2)\}_{j=2}^I = \{x_{ji,t}\}_{j=2}^I,$$

where  $x_{ji,t}$  is the expenditure share of importer  $i$  on exports of  $j$  at year  $t$  and

$$\chi_j(\delta_{i,t} | \theta_2) = \frac{1}{S} \sum_{s=1}^S \frac{\exp[\alpha_s \sigma_\alpha \ln \kappa_j + (\epsilon_s)^{\sigma_\epsilon} \delta_{ji,t}]}{1 + \sum_{l=2}^N \exp[\alpha_s \sigma_\alpha \ln \kappa_l + (\epsilon_s)^{\sigma_\epsilon} \delta_{li,t}]}$$

Uniqueness and existence of the solution is guaranteed by the fixed point argument in Berry, Levinsohn, and Pakes (1995). To solve the system, consider the fixed point of the following function:

$$\mathbf{G}(\delta_{i,t}) = \{\delta_{ji,t} + \lambda(\ln x_{ji,t} - \ln \chi_j(\delta_{i,t} | \theta_2))\}_{j=2}^I,$$

where  $\lambda$  is a parameter controlling the adjustment speed. This fixed point is obtained as the limit of the sequence:  $\delta_{i,t}^{n+1} = \mathbf{G}(\delta_{i,t}^n)$ . Numerically, we compute the sequence until  $\max_j |\ln x_{ji,t} - \ln \chi_j(\delta_{i,t} | \theta_2)| < tol$ , where  $tol$  is some small number that we discuss further below.

This step is implemented as follows. First, the initial guess  $\delta_{ij,t}^0$  in the initial iteration is set to be the logit solution  $\delta_{ji,t}^0 = \ln x_{ji,t} - \ln x_{1i,t}$ . In subsequent iterations, we use the following rule. If  $\theta_2$  is close to the parameter vector of the previous iteration, we use the system solution in the last iteration. Otherwise, we use the vector that solved the system for the same importer in the previous year (if it is the first year, we use the CES solution). Second, the speed of adjustment is initially set to  $\lambda = 3$ . If distance increases in iteration  $n$ , then we reduce  $\lambda$  by 5 percent and compute  $\delta_{i,t}^{n+1}$  again until distance decreases in the step and use the new value of  $\lambda$  until the solution is found. If  $\lambda$  falls below a minimum ( $\underline{\lambda} = 0.001$ ), then we assume no solution for the system and set the objective function to a high value. Lastly, we set  $tol = 10^{-8}$  and, every 20,000 iterations, we increase tolerance by a factor of two. This guarantees that the algorithm does not waste time on convergence for parameter values far away from the real ones, as suggested by Nevo (2000).

**Step 2:** Conditional on  $\theta_2$ , solve analytically for linear parameters directly from the minimization problem:  $\hat{\theta}_1(\theta_2) = (\mathbf{Z}'\mathbf{Z}\Phi\mathbf{Z}'\mathbf{Z}')^{-1}\mathbf{Z}'\mathbf{Z}\Phi\mathbf{Z}'\mathbf{X}$ , with  $\mathbf{X} \equiv [\ln \chi_j^{-1}(\mathbf{x}_{i,t} | \theta_2) - \ln \chi_j^{-1}(\mathbf{x}_{1,t} | \theta_2)]$ .

**Step 3:** Conditional on  $\theta_2$ , compute the vector of structural errors using  $e_{ji,t}(\theta_2) = \ln \chi_j^{-1}(\mathbf{x}_{i,t} | \theta_2) - \ln \chi_j^{-1}(\mathbf{x}_{1,t} | \theta_2) - \mathbf{Z}_{ji,t}^1 \cdot \hat{\theta}_1(\theta_2)$ .

**Step 4:** Numerically minimize the objective function to obtain estimates of  $\theta_2$ :

$$\hat{\theta}_2 \equiv \arg \min_{\theta_2} H(\theta_2) \equiv \mathbf{e}(\theta_2)' \mathbf{Z}\Phi\mathbf{Z}'\mathbf{e}(\theta_2).$$

The numerical minimization is implemented using the trust-region-reflective algorithm that requires an analytical gradient of the objective function (described below). This algorithm is intended to be more efficient in finding the local minimum within a particular attraction region. First, we solve the minimization problem using a grid of ten initial conditions randomly drawn from a uniform distribution in the parameter space. Second, we solve a final minimization problem using as initial condition the minimum solution obtained from the first-round minimization. Here, we impose a stricter convergence criteria and we reduce the tolerance level of the system solution in Step 1 to  $tol = 10^{-12}$ .

*Objective Function Gradient.*—The Jacobian of  $H(\theta_2)$  is  $\nabla H(\theta_2) = 2 \cdot \mathbf{De}(\theta_2)' \mathbf{Z}\Phi\mathbf{Z}'\mathbf{e}(\theta_2)$  where  $\mathbf{De}(\theta_2) = \left[ \frac{\partial e_{ji,t}}{\partial \theta_{21}} \dots \frac{\partial e_{ji,t}}{\partial \theta_{2L}} \right]_{ijt}$  is the stacked matrix of Jacobian vectors of the structural error from Step 3. By the envelope theorem, the Jacobian is  $\mathbf{De}_{i,t}(\theta_2) = D\delta_{i,t}(\theta_2) - D\delta_{1,t}(\theta_2)$  because  $\hat{\theta}_1(\theta_2)$  is obtained from

the analytical minimization of the inner problem restricted to a particular level of  $\theta_2$ . For each importer-year, the implicit function theorem implies that

$$D\delta_{i,t}(\theta_2) = \begin{bmatrix} \frac{\partial \delta_{2i,t}}{\partial \theta_{21}} & \cdots & \frac{\partial \delta_{2i,t}}{\partial \theta_{2L}} \\ \vdots & \ddots & \vdots \\ \frac{\partial \delta_{Ni,t}}{\partial \theta_{21}} & \cdots & \frac{\partial \delta_{Ni,t}}{\partial \theta_{2L}} \end{bmatrix} = - \begin{bmatrix} \frac{\partial \bar{\chi}_2}{\partial \delta_{2i,t}} & \cdots & \frac{\partial \bar{\chi}_2}{\partial \delta_{Ni,t}} \\ \vdots & \ddots & \vdots \\ \frac{\partial \bar{\chi}_N}{\partial \delta_{2i,t}} & \cdots & \frac{\partial \bar{\chi}_N}{\partial \delta_{Ni,t}} \end{bmatrix}^{-1} \begin{bmatrix} \frac{\partial \bar{\chi}_2}{\partial \theta_{21}} & \cdots & \frac{\partial \bar{\chi}_2}{\partial \theta_{2L}} \\ \vdots & \ddots & \vdots \\ \frac{\partial \bar{\chi}_N}{\partial \theta_{21}} & \cdots & \frac{\partial \bar{\chi}_N}{\partial \theta_{2L}} \end{bmatrix},$$

where

$$\frac{\partial \chi_j}{\partial \delta_{li,t}} = \begin{cases} -\frac{1}{S} \sum_{s=1}^S (\epsilon_s)^{\sigma_\epsilon} \cdot x_{ji,t}(\alpha_s, \epsilon_s) x_{li,t}(\alpha_s, \epsilon_s) & \text{if } l \neq j \\ \frac{1}{S} \sum_{s=1}^S (\epsilon_s)^{\sigma_\epsilon} \cdot x_{ji,t}(\alpha_s, \epsilon_s) (1 - x_{ji,t}(\alpha_s, \epsilon_s)) & \text{if } l = j \end{cases},$$

$$\frac{\partial \chi_j}{\partial \sigma_\epsilon} = \frac{1}{S} \sum_{s=1}^S (\ln \epsilon_s) (\epsilon_s)^{\sigma_\epsilon} \cdot x_{ji,t}(\alpha_s, \epsilon_s) \cdot \left[ \delta_{ji,t} - \sum_{l=2}^N x_{li,t}(\alpha_s, \epsilon_s) \cdot \delta_{li,t} \right],$$

$$\frac{\partial \chi_j}{\partial \sigma_\alpha} = \frac{1}{S} \sum_{s=1}^S \alpha_s \cdot x_{ji,t}(\alpha_s, \epsilon_s) \cdot \left[ \ln \kappa_i - \sum_{l=2}^N x_{li,t}(\alpha_s, \epsilon_s) \cdot \ln \kappa_l \right].$$

## APPENDIX C: SAMPLE OF COUNTRIES

TABLE A1—LIST OF EXPORTING COUNTRIES

Abbreviation	Exporter	log (p.c. GDP) [USA = 0]
AUS	Australia	-0.246
AUT	Austria	-0.249
BLX	Belgium-Luxembourg	-0.261
BRA	Brazil	-1.666
BGR	Bulgaria	-1.603
CAN	Canada	-0.211
CHN	China	-2.536
CZE	Czech Republic	-0.733
DNK	Denmark	-0.303
BAL	Estonia-Latvia	-1.475
FIN	Finland	-0.522
FRA	France	-0.398
DEU	Germany	-0.290
GRC	Greece	-0.760
HUN	Hungary	-1.121
IND	India	-3.214
IDN	Indonesia	-2.284
IRL	Ireland	-0.574
ITA	Italy	-0.332
JPN	Japan	-0.183

(Continued)

TABLE A1—LIST OF EXPORTING COUNTRIES (*Continued*)

Abbreviation	Exporter	log (p.c. GDP) [USA = 0]
LTU	Lithuania	-1.526
MEX	Mexico	-1.263
NLD	Netherlands	-0.352
POL	Poland	-1.428
PRT	Portugal	-0.830
KOR	Republic of Korea	-0.823
RoW	Rest of World	-2.286
ROU	Romania	-1.816
RUS	Russia	-0.954
SVK	Slovak Republic	-1.102
SVN	Slovenia	-0.728
ESP	Spain	-0.644
SWE	Sweden	-0.367
TWN	Taiwan	-0.584
TUR	Turkey	-1.305
GBR	United Kingdom	-0.436
USA	United States	0.000

APPENDIX D: COUNTERFACTUAL ANALYSIS

A. Preliminaries

In the counterfactual analysis of Section VI, we use the complete trade matrix for the 37 exporters listed in Table A1. In order to reconcile theory and data, we incorporate trade imbalances as follows. For each country, we define  $\rho_{j,t}$  as the difference between aggregate gross expenditure and aggregate gross production. We proceed under the assumption that trade imbalances remain constant at their observed level in terms of the factor price of the reference country. Here, the reference country is the United States ( $j = 1$ ) such that its factor price is normalized to 1,  $\hat{w}_1 = 1$ . In particular, the market clearing condition in (15) becomes

$$(62) \quad \sum_{i=1}^I \hat{x}_{ji,t} x_{ji,t} ((\hat{w}_i \hat{v}_i) y_{i,t} + \rho_{i,t}) = (\hat{w}_j \hat{v}_j) y_{j,t}, \quad \text{for } j = 2, \dots, I$$

where

$$(63) \quad \hat{x}_{ji,t} x_{ji,t} = \frac{1}{S} \sum_{s=1}^S \frac{\exp [\alpha_s \sigma_\alpha \ln \kappa_j + (\epsilon_s)^{\sigma_\epsilon} (\chi_j^{-1}(\mathbf{x}_{i,t} | \boldsymbol{\theta}_2) - \bar{\epsilon} \ln(\hat{w}_j \hat{\tau}_{ji}))]}{1 + \sum_{l=2}^N \exp [\alpha_s \sigma_\alpha \ln \kappa_l + (\epsilon_s)^{\sigma_\epsilon} (\chi_l^{-1}(\mathbf{x}_{i,t} | \boldsymbol{\theta}_2) - \bar{\epsilon} \ln(\hat{w}_l \hat{\tau}_{li}))]}$$

Notice that, by construction,  $\sum_{i=1}^I \rho_{i,t} = 0$ . Thus, the solution of the system of  $I - 1$  equations above implies that the market clearing condition for the reference country is automatically satisfied.

B. Algorithm

To compute the vector  $\hat{\mathbf{w}} = \{\hat{w}_j\}_{j=2}^I$  that solves system (62), we use the same algorithm as in Alvarez and Lucas (2007).

**Step 0:** Initial guess:  $\hat{\mathbf{w}}^k = [1, \dots, 1]$  if  $k = 0$ .

**Step 1:** Conditional on  $\hat{\mathbf{w}}^k$ , compute  $\hat{x}_{ji,t}x_{ji,t}$  according to (63).

**Step 2:** Compute the excess labor demand as

$$F_j(\hat{\mathbf{w}}^k) \equiv \frac{1}{y_{j,t}} \left[ -(\hat{w}_j \hat{v}_j) y_{j,t} + \sum_{i=1}^I \hat{x}_{ji,t} x_{ji,t} ((\hat{w}_i \hat{v}_i) y_{i,t} + \rho_{i,t}) \right]$$

where we divide by  $y_{j,t}$  to scale excess demand by country size.

**Step 3:** If  $\max_j |F_j(\hat{\mathbf{w}}^k)| < tol$ , then stop the algorithm. (In practice we set  $tol = 10^{-8}$  here.) Otherwise, return to Step 1 with new factor prices computed as

$$\hat{w}_j^{k+1} = \hat{w}_j^k + \mu F_j(\hat{\mathbf{w}}^k),$$

where  $\mu$  is a positive constant. Intuitively, this updating rule increases the price of those factors with a positive excess demand.

### C. Welfare

By Proposition 3, we can compute welfare changes in any country  $i$  by solving for  $e(\cdot, U_i^t)$ . To do so, we guess that for all  $\omega \equiv \{\omega_l\}$ ,

$$(64) \quad e(\omega, U_i^t) = (y_i) \frac{\exp\left(\int \frac{1}{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} \ln \left[\sum_{l=1}^I (\kappa_l)^{\sigma_{\alpha\alpha}} (\omega_l)^{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} dF(\alpha, \epsilon)\right]\right)}{\exp\left(\int \frac{1}{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} \ln \left[\sum_{l=1}^I (\kappa_l)^{\sigma_{\alpha\alpha}} ((\omega_{li,t})')^{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} dF(\alpha, \epsilon)\right]\right)}.$$

We then check that our guess satisfies (17) and (18) if  $\chi$  satisfies (28). By equations (19) and (64), welfare changes must therefore satisfy

$$\Delta W_i = \frac{(y_i)'/\exp\left(\int \frac{1}{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} \ln \left[\sum_{l=1}^I (\kappa_l)^{\sigma_{\alpha\alpha}} ((\omega_{li,t})')^{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} dF(\alpha, \epsilon)\right]\right)}{y_i/\exp\left(\int \frac{1}{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} \ln \left[\sum_{l=1}^I (\kappa_l)^{\sigma_{\alpha\alpha}} (\chi_l^{-1}(\mathbf{x}_{i,t}))^{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} dF(\alpha, \epsilon)\right]\right)} - 1.$$

Using the fact that  $(y_i)'/y_i = \hat{w}_i$  and  $(\omega_{li,t})' = \hat{w}_l \hat{\tau}_{li} \chi_l^{-1}(\mathbf{x}_{i,t})$ , this finally leads to

$$\Delta W_i = (\hat{w}_i) \frac{\exp\left(\int \frac{1}{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} \ln \left[\sum_{l=1}^I (\kappa_l)^{\sigma_{\alpha\alpha}} (\chi_l^{-1}(\mathbf{x}_{i,t}))^{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} dF(\alpha, \epsilon)\right]\right)}{\exp\left(\int \frac{1}{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} \ln \left[\sum_{l=1}^I (\kappa_l)^{\sigma_{\alpha\alpha}} (\hat{w}_l \hat{\tau}_{li} \chi_l^{-1}(\mathbf{x}_{i,t}))^{-(\bar{\epsilon} \epsilon^{\sigma_\epsilon})} dF(\alpha, \epsilon)\right]\right)} - 1,$$

with  $\{\hat{w}_l\}$  obtained from the algorithm in subsection B above.

### D. Confidence Intervals

The confidence intervals for the counterfactual analysis are computed with the following bootstrap procedure. (i) Draw parameter values from the asymptotic

distribution of the GMM estimator:  $\theta(b) \sim N(\hat{\theta}, \widehat{AVar}(\hat{\theta}))$ . (ii) Compute  $\chi^{-1}(\mathbf{x}_{i,t} | \theta_2(b))$  using the algorithm described in Step 1 of Appendix B, Section C. (iii) Compute the counterfactual exercise with  $\theta(b)$  and  $\chi^{-1}(\mathbf{x}_{i,t} | \theta_2(b))$  using the algorithm described in Section B of Appendix D. (iv) Repeat these three steps for  $b = 1, \dots, 200$ . The bootstrap confidence interval corresponds to  $[EV^{(0.025)}, EV^{(0.975)}]$  where  $EV^{(\alpha)}$  denotes the  $\alpha$ th quantile value of the equivalent variation obtained across the set of 200 parameter draws.

### E. Additional Results

TABLE A2—WELFARE GAINS FROM CHINESE INTEGRATION SINCE 1995: ALL COUNTRIES, 2007

Exporter	CES (standard gravity)		Mixed CES	
	Welfare gains	95% confidence interval	Welfare gains	95% confidence interval
Australia	0.144	(0.109, 0.243)	0.225	(0.136, 0.598)
Austria	0.058	(0.043, 0.100)	0.102	(0.055, 0.296)
Belgium-Luxembourg	0.056	(0.042, 0.097)	0.108	(0.044, 0.312)
Brazil	0.071	(0.054, 0.121)	0.058	(0.049, 0.191)
Bulgaria	0.061	(0.045, 0.106)	-0.005	(-0.077, 0.078)
Canada	0.053	(0.039, 0.092)	0.098	(0.044, 0.301)
China	1.039	(0.788, 1.740)	1.544	(1.006, 4.284)
Czech Republic	0.151	(0.112, 0.262)	0.209	(0.140, 0.570)
Denmark	0.014	(0.010, 0.026)	0.034	(-0.009, 0.137)
Estonia-Latvia	0.081	(0.061, 0.140)	0.043	(0.033, 0.190)
Finland	0.100	(0.075, 0.171)	0.154	(0.092, 0.437)
France	0.030	(0.023, 0.052)	0.057	(0.029, 0.214)
Germany	0.122	(0.092, 0.208)	0.201	(0.117, 0.519)
Greece	0.004	(0.003, 0.006)	0.018	(-0.003, 0.114)
Hungary	0.214	(0.161, 0.370)	0.208	(0.169, 0.555)
India	0.126	(0.094, 0.218)	0.022	(-0.141, 0.185)
Indonesia	0.026	(0.019, 0.047)	-0.061	(-0.415, 0.016)
Ireland	0.135	(0.101, 0.234)	0.150	(0.116, 0.379)
Italy	0.008	(0.006, 0.015)	0.035	(0.002, 0.161)
Japan	0.095	(0.072, 0.162)	0.186	(0.093, 0.599)
Lithuania	0.065	(0.049, 0.110)	0.022	(-0.003, 0.114)
Mexico	0.121	(0.090, 0.211)	0.099	(0.082, 0.360)
Netherlands	0.043	(0.032, 0.076)	0.068	(0.019, 0.157)
Poland	0.086	(0.064, 0.151)	0.040	(0.030, 0.210)
Portugal	0.050	(0.038, 0.081)	0.055	(0.043, 0.141)
Republic of Korea	0.298	(0.226, 0.500)	0.399	(0.273, 0.951)
Rest of World	0.293	(0.221, 0.493)	0.105	(-0.160, 0.384)
Romania	-0.005	(-0.009, -0.004)	-0.077	(-0.367, -0.013)
Russia	0.105	(0.079, 0.180)	0.103	(0.085, 0.221)
Slovak Republic	0.116	(0.087, 0.200)	0.120	(0.093, 0.343)
Slovenia	0.012	(0.008, 0.022)	0.020	(0.007, 0.078)
Spain	0.075	(0.056, 0.127)	0.112	(0.071, 0.331)
Sweden	0.076	(0.057, 0.130)	0.113	(0.072, 0.315)
Taiwan	0.695	(0.531, 1.140)	0.946	(0.651, 2.146)
Turkey	0.024	(0.018, 0.043)	0.019	(0.015, 0.086)
United Kingdom	0.014	(0.010, 0.024)	0.022	(0.002, 0.094)
United States	0.034	(0.025, 0.062)	0.071	(0.035, 0.237)

Notes: Estimates of welfare changes (computed as the minus of the equivalent variation) from replacing China's trade costs to all other countries in 2007 at their 1995 levels. CES (standard gravity) and mixed CES report these welfare changes obtained using the factor demand system in panels A and C, respectively, of Table 2. Ninety-five percent confidence intervals computed using the bootstrap procedure documented in Appendix D.

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